



Adaptive Channel Sparsity for Federated Learning under System Heterogeneity

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DEPARTMENT OF
COMPUTER AND INFORMATION SCIENCE

Quick Preview of Our Work

Flado: Adaptive Channel Sparsity for Federated Learning under System Heterogeneity

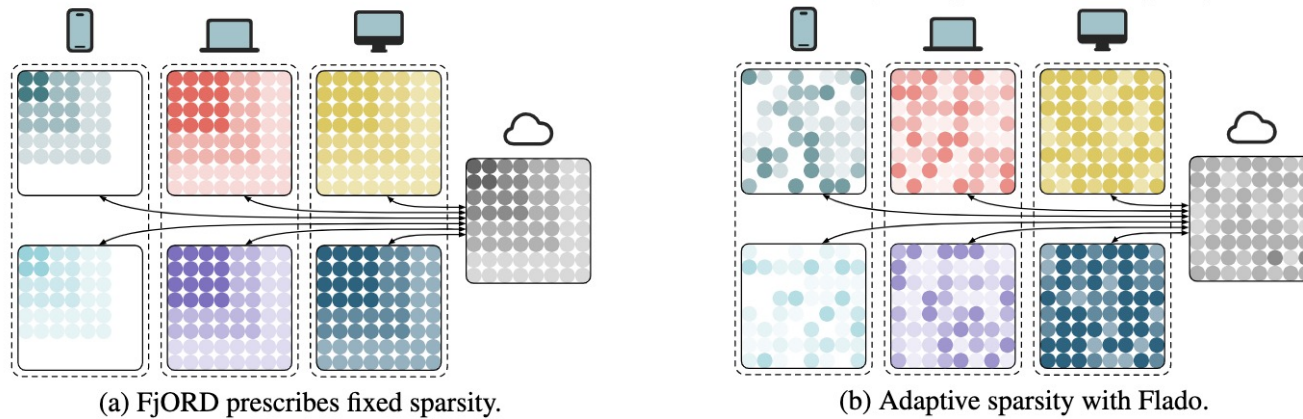


Figure 1. Comparing FjORD and the proposed method *Flado*.

Background of Federated Learning



Figure 2. European GDPR legislation

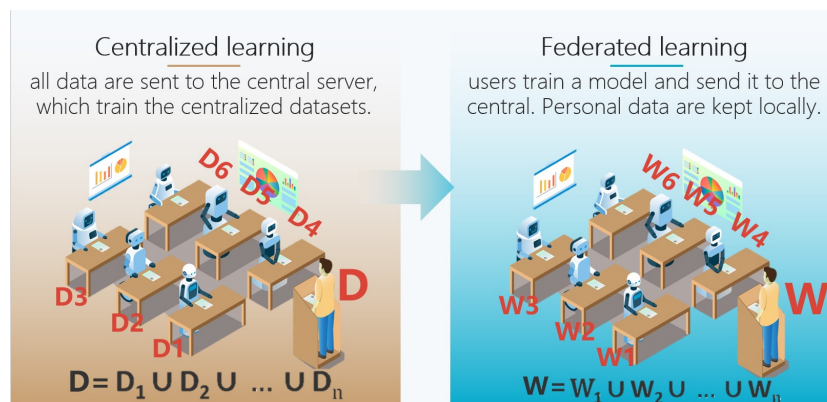


Figure 3. Comparing centralized and federated learning.

Due to increasingly stringent privacy protection legislations, the traditional centralized data analysis is no longer applicable for data located on massive edge devices.

image source: <https://www.mn.uio.no/ifi/studier/masteroppgaver/nd/new-aggregation-methods-in-federated-learning.html>



Addressing System Heterogeneity in FL

System Heterogeneity

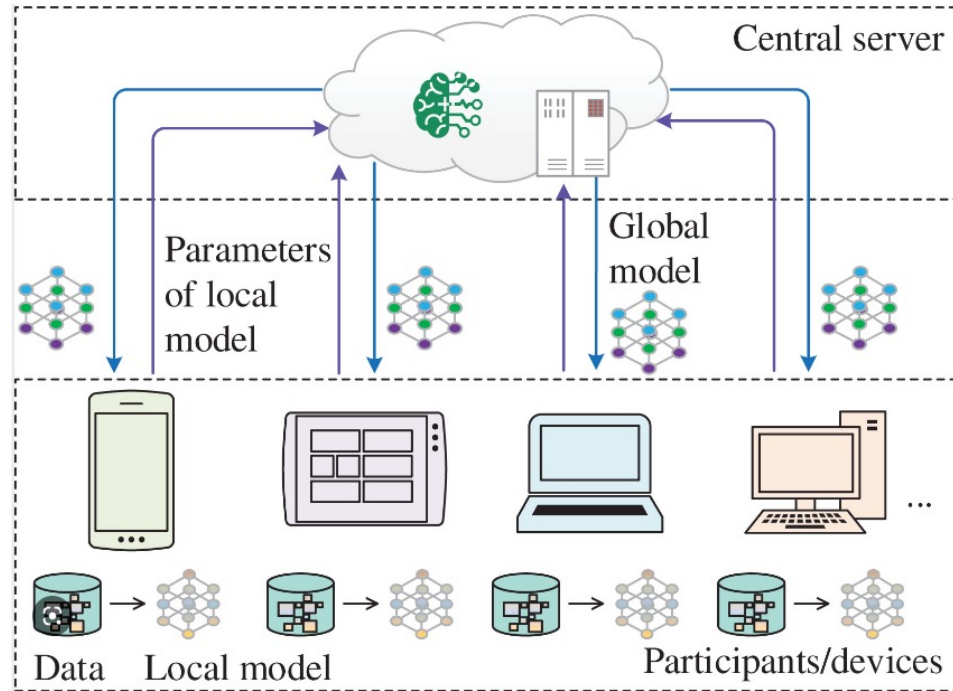


Figure 4. Participating clients may have different computing capabilities.

Addressing System Heterogeneity in FL

Existing works

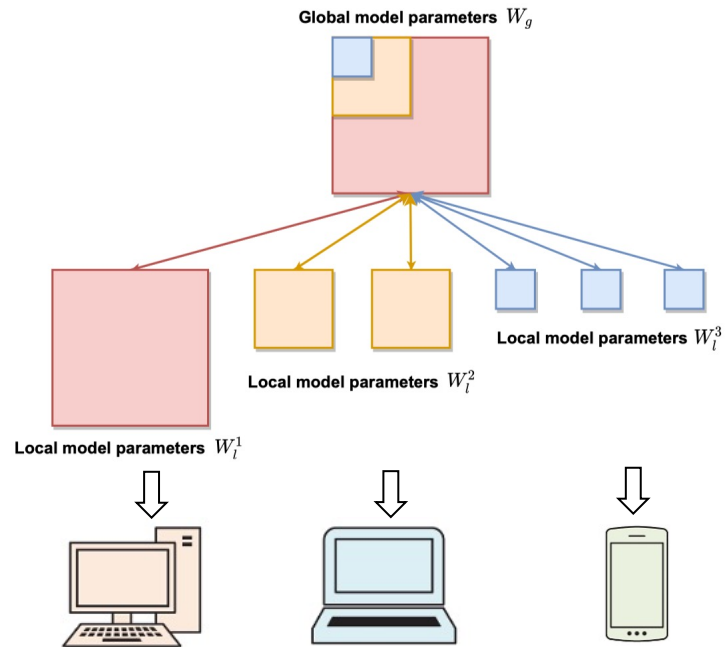


Figure 5. A concept illustration of HeteroFL^[1]

HeteroFL: Slices submodels to adapt to devices with different computing capabilities

[1] Diao, Enmao et al. "HeteroFL: Computation and Communication Efficient Federated Learning for Heterogeneous Clients", ICLR2021

Addressing System Heterogeneity in FL

Existing works

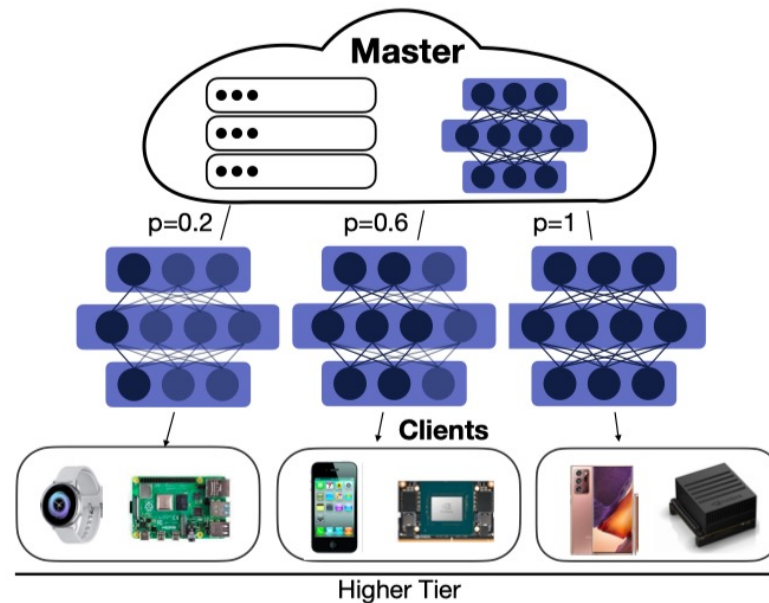


Figure 6. A concept illustration of FjORD^[1]

FjORD: customizes the maximal model width and applies ordered dropout in each training step.

[1] Horvath et al. "Fjord: Fair and accurate federated learning under heterogeneous targets with ordered dropout.". NeurIPS2021.

Addressing System Heterogeneity in FL

Limitations of existing works

System heterogeneity

Data heterogeneity

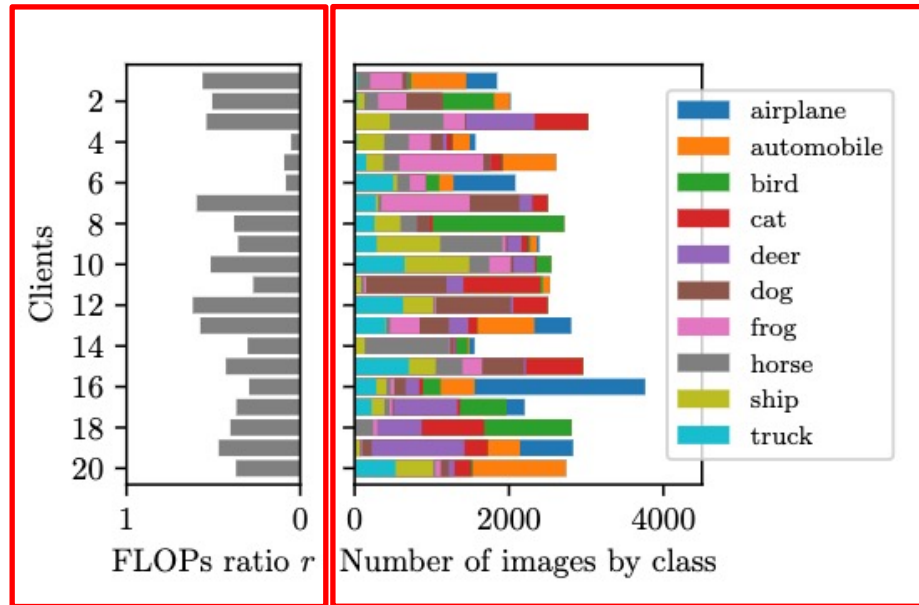


Figure 7. Existing works focus on system heterogeneity, but ignore the impact of local data distribution.

Limitations:

- Existing works prescribe a *coordinate-wise* sparsity pattern but ignored different data distributions among clients, which may cause conflicting gradient updates
- A fixed sparsity scheme could hinder collaborative training among clients, as some neurons are deactivated permanently.

Addressing System Heterogeneity in FL

Intuition: neurons may specialize to distinct features

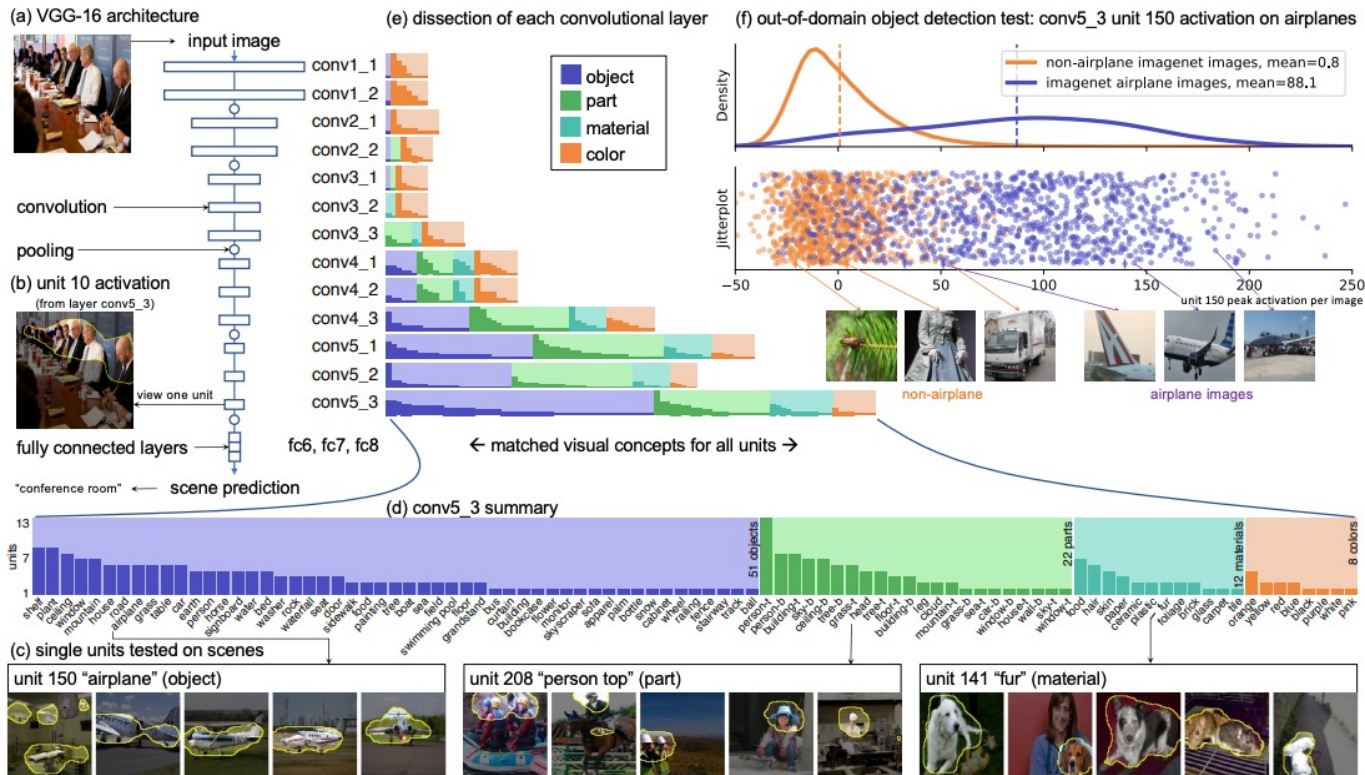


Figure 8. An illustration of single neuron activation on different objects within a VGG-16 scene classifier^{[1][2]}

[1] Bau David et al. "Understanding the role of individual units in a deep neural network." *Proceedings of the National Academy of Sciences*, 2020.
 [2] Zhou Bolei et al. Interpreting deep visual representations via network dissection. *IEEE transactions on pattern analysis and machine intelligence*, 2018.

Addressing System Heterogeneity in FL

Observation: local gradient update is contingent on data distribution

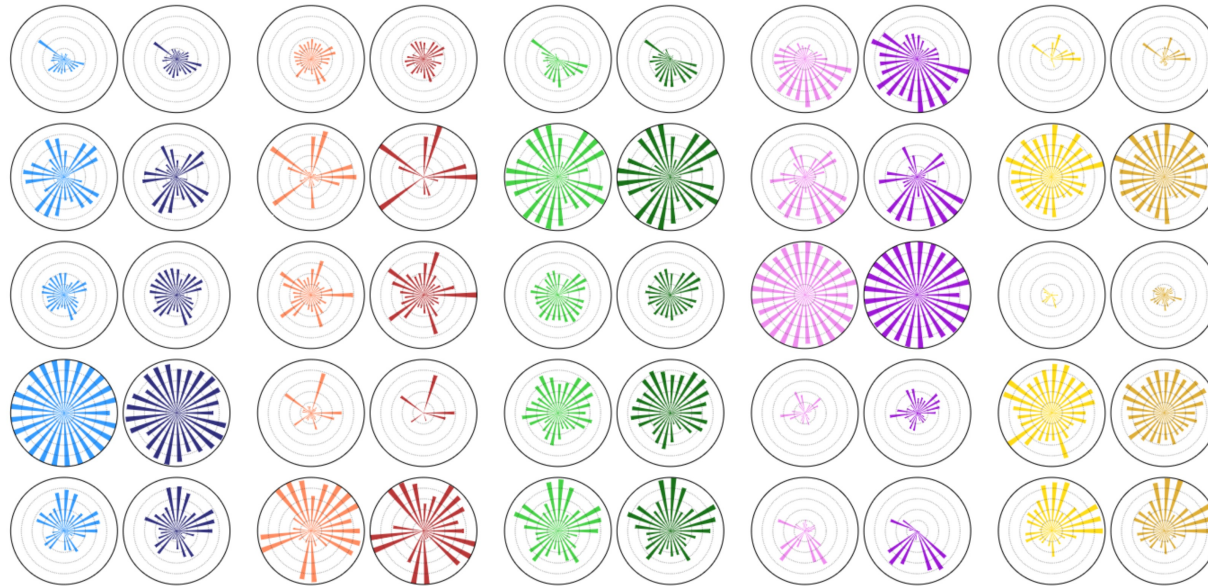


Figure 9. Similarity matrix of clients' gradient update direction

Observation: The clients allocated with the same digits shared similar update patterns, while different client pairs update direction is quite dispersed.

Addressing System Heterogeneity in FL

Motivation: can we foster collaboration by tailoring sparsity for each client?

Insights: It turns out that clients that shared similar data distributions tend to have similar updates, and by contrast different data distributions resulted in disparate updates.

Motivation: Can we **concentrate training effort** on neurons that specialize to the data distribution of the client, while paying less attention to neurons that are less relevant to the client?



Adaptive Channel Sparsity for Federated Learning

Proposed Method *Flado*: Federated Learning with Adaptive Dropout

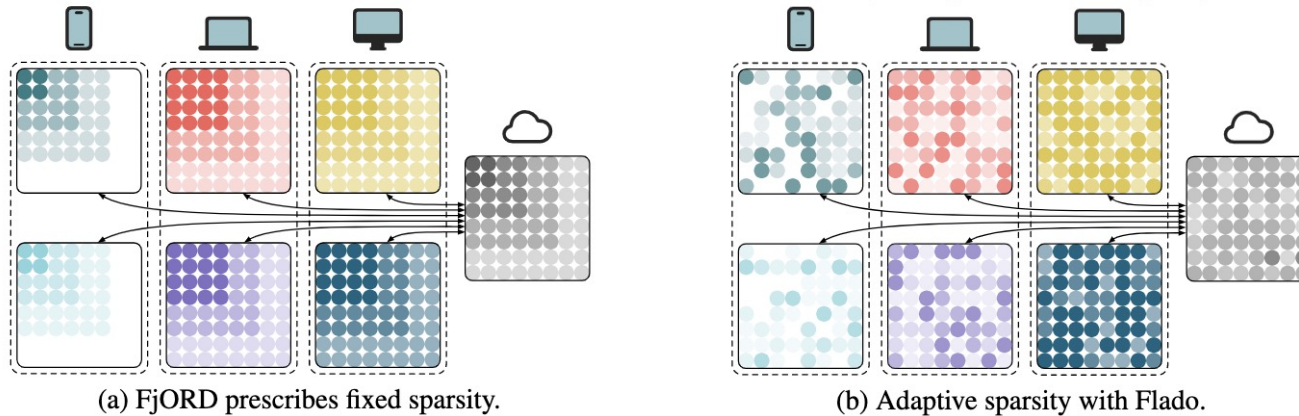


Figure 10. Comparing FjORD and the proposed method *Flado*.

How to design the adaptive channel sparsity?

Challenges:

- pruning channel neurons would cause them to make no contribution later.
- prescribing a fixed sparsity scheme to channels can be suboptimal
- data heterogeneity causes clients to specialize to train different neurons

Adaptive Channel Sparsity for Federated Learning

Sparsity-driven Trajectory Alignment

$$J(\mathbf{z}) = \mathbf{P}\mathbf{H}\mathbf{D}\mathbf{z},$$

fast Johnson-Lindenstrauss transform (FJLT)

$$\max_{\mathbf{p}_c} \mathbb{E}_{\mathbf{b}_c \sim \mathcal{B}(\mathbf{p}_c)}$$

$$\text{cossim}(J(\Delta\boldsymbol{\theta}^{(t)}), J(\nabla_{\boldsymbol{\theta}^{(t)}} \ell_c(\mathbf{b}_c \circ \boldsymbol{\theta}^{(t)}))),$$

$$s.t. g_c(r_c, \mathbf{p}_c) \geq 0. \quad \text{FLOPs budget constraint}$$

FLOPs constraint

$$g_c(r_c, \mathbf{p}_c) = r_c - \text{flops}(\ell_c, \mathbf{p}_c) / \text{flops}(\ell_c, \mathbf{1}),$$



Adaptive Channel Sparsity for Federated Learning

Main Results

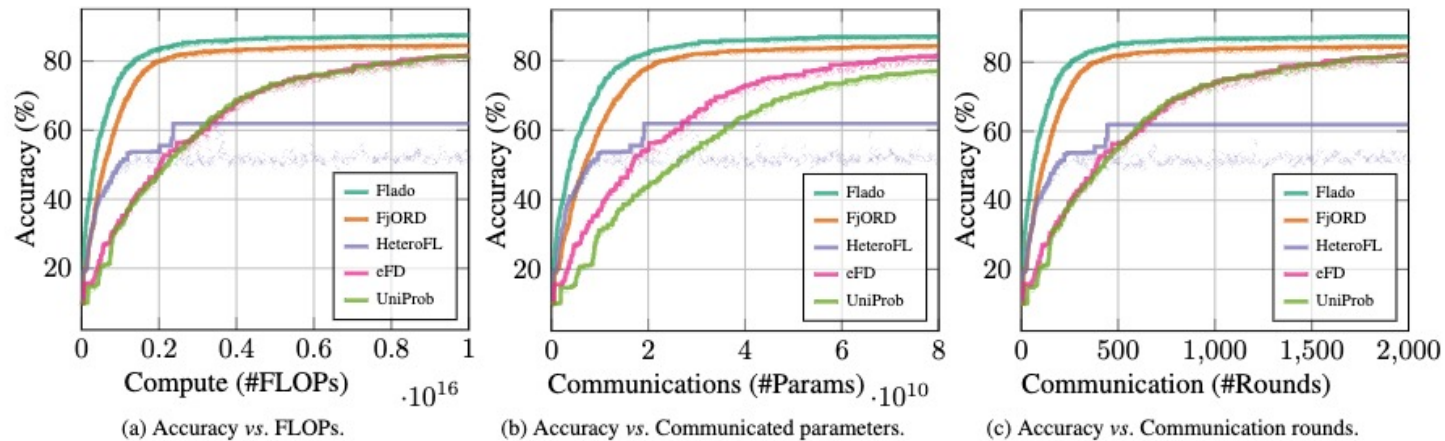


Figure 11. Comparison of convergence curves on CIFAR10.

Flado attains consistently higher converged accuracies.

Adaptive Channel Sparsity for Federated Learning

Main Results

Table 1. Comparing the sparse FL algorithms on converged accuracies, computation and communication costs.

| Method | CIFAR-10 | | | Permitting -5% accuracy budget from Flado | | | Permitting -10% accuracy budget from Flado | | |
|----------|---------------------------|-------------------------------|--------------------------------|---|---------------------------------|-------------------------------|--|--------------------------------|-------------------------------|
| | Accuracy | Δ FLOPs | Δ Comm. Params | Rounds | FLOPs | Comm.Params | Rounds | FLOPs | Comm. Params |
| HeteroFL | 53.83% \pm 3.66% | 2.13 P \pm 14.67 T | 18.08 G \pm 124.45 M | — | — | — | — | — | — |
| UniProb | 80.91% \pm 0.61% | -2.90 P \pm 2.12 P | -14.01 G \pm 18.03 G | — | — | — | 1329.5 \pm 2.9 | 6.21 P \pm 14.48 T | 75.59 G \pm 176.28 M |
| eFD | 81.82% \pm 0.31% | -113.08 T \pm 91.82 T | -34.02 G \pm 1.09 G | — | — | — | 1287.5 \pm 5.2 | 6.01 P \pm 25.31 T | 51.56 G \pm 218.57 M |
| FjORD | 84.38% \pm 0.18% | -6.59 P \pm 76.82 T | -47.06 G \pm 657.26 M | 562.5 \pm 5.76 | 2.63 P \pm 14.48 T | 31.98 G \pm 176.28 M | 314.5 \pm 4.6 | 1.47 P \pm 22.77 T | 17.88 G \pm 277.20 M |
| Flado | 87.24% \pm 0.17% | -7.21 P \pm 6.18 T | -87.71 G \pm 75.17 M | 330.5 \pm 3.45 | 1.54 P \pm 8.99 T | 18.79 G \pm 108.93 M | 215.5 \pm 2.3 | 1.01 P \pm 11.71 T | 12.25 G \pm 142.62 M |
| Method | SVHN | | | Permitting -2% accuracy budget from Flado | | | Permitting -5% accuracy budget from Flado | | |
| | Accuracy | Δ FLOPs | Δ Comm. Params | Rounds | FLOPs | Comm. Params | Rounds | FLOPs | Comm. Params |
| HeteroFL | 89.07% \pm 0.23% | 390.35 T \pm 1.02 T | 38.63 G \pm 103.75 M | — | — | — | 163.5 \pm 1.7 | 55.28 T \pm 647.74 G | 5.47 G \pm 64.11 M |
| UniProb | 90.39% \pm 0.07% | -299.57 T \pm 83.02 T | -22.48 G \pm 8.22 G | — | — | — | 426.5 \pm 2.9 | 139.25 T \pm 1012.26 G | 18.07 G \pm 131.38 M |
| eFD | 91.11% \pm 0.06% | -226.29 T \pm 40.39 T | -39.24 G \pm 5.24 G | 1540.5 \pm 2.3 | 502.85 T \pm 804.65 G | 51.35 G \pm 83.41 M | 430.5 \pm 5.2 | 140.55 T \pm 1.75 T | 14.35 G \pm 182.26 M |
| FjORD | 92.36% \pm 0.04% | -399.73 T \pm 10.61 T | -34.31 G \pm 1.08 G | 667.5 \pm 3.5 | 217.86 T \pm 1.18 T | 28.29 G \pm 156.45 M | 253.5 \pm 1.7 | 82.75 T \pm 625.16 G | 10.74 G \pm 81.18 M |
| Flado | 92.90% \pm 0.04% | -354.03 T \pm 1.46 T | -45.98 G \pm 194.05 M | 442.5 \pm 2.9 | 144.48 T \pm 1012.26 G | 18.75 G \pm 131.38 M | 199.5 \pm 2.9 | 65.14 T \pm 1012.26 G | 8.45 G \pm 131.38 M |
| Method | Fashion-MNIST | | | Permitting -5% accuracy budget from Flado | | | Permitting -10% accuracy budget from Flado | | |
| | Accuracy | Δ FLOPs | Δ Comm. Params | Rounds | FLOPs | Comm. Params | Rounds | FLOPs | Comm. Params |
| UniProb | 83.00% \pm 0.11% | 1.83 P \pm 2.84 T | 44.38 G \pm 69.06 M | — | — | — | 698.5 \pm 1.7 | 656.28 T \pm 1.76 T | 15.56 G \pm 42.67 M |
| eFD | 84.94% \pm 0.09% | -1.18 P \pm 3.66 T | -33.68 G \pm 88.83 M | — | — | — | 410.5 \pm 2.3 | 386.11 T \pm 2.29 T | 6.24 G \pm 38.14 M |
| FjORD | 85.54% \pm 0.06% | -253.89 T \pm 51.17 T | +7.49 G \pm 847.86 M | — | — | — | 366.5 \pm 1.1 | 344.15 T \pm 1.21 T | 8.16 G \pm 29.45 M |
| HeteroFL | 87.29% \pm 0.17% | -1.35 P \pm 3.66 T | -36.75 G \pm 88.83 M | 498.5 \pm 4.6 | 491.32 T \pm 4.69 T | 7.66 G \pm 74.94 M | 122.5 \pm 5.8 | 115.10 T \pm 5.56 T | 2.73 G \pm 134.95 M |
| Flado | 90.58% \pm 0.09% | -1.05 P \pm 147.24 T | -11.56 G \pm 2.30 G | 354.5 \pm 4.0 | 333.07 T \pm 3.93 T | 7.90 G \pm 95.42 M | 81.5 \pm 1.7 | 80.33 T \pm 1.84 T | 1.25 G \pm 29.45 M |

Flado is more efficient than competing methods on computation and communication cost.



Adaptive Channel Sparsity for Federated Learning

Main Results

Table 2. Comparing the sparse FL algorithms under increasing level of data heterogeneity.

| $\alpha = \infty$ | Accuracy | Δ FLOPs | Δ Comm. Params |
|-------------------|---------------------------|------------------------------|--------------------------------|
| HeteroFL | 83.20% \pm 0.42% | 2.49 P \pm 14.67 T | 21.13 G \pm 124.45 M |
| UniProb | 85.38% \pm 0.22% | +0.80 P \pm 2.02 P | +31.49 G \pm 17.14 G |
| eFD | 85.86% \pm 0.21% | -0.87 P \pm 98.72 T | -40.32 G \pm 1.17 G |
| FjORD | 87.58% \pm 0.09% | -6.43 P \pm 36.67 T | -44.91 G \pm 313.70 M |
| Flado | 89.16% \pm 0.08% | -7.13 P \pm 58.68 T | -86.80 G \pm 714.29 M |
| $\alpha = 5$ | Accuracy | Δ FLOPs | Δ Comm. Params |
| HeteroFL | 82.51% \pm 0.34% | 5.17 P \pm 14.67 T | 43.86 G \pm 124.45 M |
| UniProb | 84.82% \pm 0.17% | +1.69 P \pm 14.67 T | +39.67 G \pm 124.45 M |
| eFD | 85.69% \pm 0.25% | -1.75 P \pm 14.48 T | -48.29 G \pm 176.28 M |
| FjORD | 86.92% \pm 0.17% | -5.38 P \pm 14.47 T | -32.17 G \pm 123.96 M |
| Flado | 88.85% \pm 0.10% | -6.97 P \pm 14.48 T | -84.81 G \pm 176.28 M |
| $\alpha = 0.05$ | Accuracy | Δ FLOPs | Δ Comm. Params |
| HeteroFL | 28.06% \pm 5.04% | 2.27 P \pm 14.67 T | 19.29 G \pm 124.45 M |
| UniProb | 63.05% \pm 1.14% | +0.60 P \pm 14.67 T | +15.51 G \pm 124.45 M |
| eFD | 62.84% \pm 1.20% | -0.34 P \pm 13.10 T | -49.88 G \pm 159.45 M |
| FjORD | 77.64% \pm 0.91% | -10.54 P \pm 14.44 T | -82.39 G \pm 124.11 M |
| Flado | 79.14% \pm 1.12% | -5.92 P \pm 14.48 T | -72.07 G \pm 176.28 M |

Flado tolerates aggressive data heterogeneity.



Adaptive Channel Sparsity for Federated Learning

Main Results

Table 3. Comparing the sparse FL algorithms under increasing level of system heterogeneity.

| $\mathcal{U}(0.64, 0.64)$ | Accuracy | Δ FLOPs | Δ Comm. Params |
|---------------------------|---------------------------|-------------------------------|--------------------------------|
| FjORD | 87.01% \pm 0.11% | 15.26 P \pm 23.83 T | 112.89 G \pm 176.28 M |
| HeteroFL | 87.43% \pm 0.09% | -4.72 P \pm 24.22 T | -47.32 G \pm 150.50 M |
| UniProb | 87.44% \pm 0.13% | -3.11 P \pm 23.79 T | -4.81 G \pm 176.28 M |
| eFD | 88.26% \pm 0.09% | -2.18 P \pm 23.82 T | -29.42 G \pm 149.96 M |
| Flado | 88.82% \pm 0.14% | -11.88 P \pm 23.83 T | -25.67 G \pm 176.28 M |

| $\mathcal{U}(0.32, 0.64)$ | Accuracy | Δ FLOPs | Δ Comm. Params |
|---------------------------|---------------------------|------------------------------|-------------------------------|
| HeteroFL | 58.91% \pm 4.23% | 2.96 P \pm 19.11 T | 21.40 G \pm 138.38 M |
| eFD | 85.55% \pm 0.15% | +227.50 T \pm 18.92 T | +1.89 G \pm 138.11 M |
| UniProb | 86.08% \pm 0.31% | -2.81 P \pm 18.84 T | -1.70 G \pm 176.28 M |
| FjORD | 86.43% \pm 0.14% | -102.70 T \pm 18.84 T | -960.70 M \pm 176.28 M |
| Flado | 87.88% \pm 0.13% | -8.98 P \pm 18.84 T | +3.04 G \pm 176.28 M |

| $\mathcal{U}(0.16, 0.64)$ | Accuracy | Δ FLOPs | Δ Comm. Params |
|---------------------------|---------------------------|------------------------------|--------------------------------|
| HeteroFL | 57.64% \pm 4.65% | 2.52 P \pm 16.53 T | 20.02 G \pm 131.09 M |
| eFD | 83.82% \pm 0.28% | +842.98 T \pm 16.44 T | +6.78 G \pm 131.05 M |
| UniProb | 83.89% \pm 0.43% | -331.42 T \pm 16.35 T | +25.80 G \pm 176.28 M |
| FjORD | 85.84% \pm 0.19% | -6.83 P \pm 16.35 T | -73.60 G \pm 176.28 M |
| Flado | 86.91% \pm 0.16% | -5.09 P \pm 16.34 T | -54.90 G \pm 176.28 M |

| $\mathcal{U}(0.08, 0.64)$ | Accuracy | Δ FLOPs | Δ Comm. Params |
|---------------------------|---------------------------|------------------------------|--------------------------------|
| HeteroFL | 57.39% \pm 4.20% | 2.35 P \pm 15.36 T | 19.39 G \pm 126.96 M |
| eFD | 81.45% \pm 0.59% | +999.93 T \pm 15.02 T | +8.46 G \pm 126.61 M |
| UniProb | 81.70% \pm 0.52% | -186.77 T \pm 15.10 T | +29.60 G \pm 176.28 M |
| FjORD | 84.58% \pm 0.19% | -6.62 P \pm 15.10 T | -77.24 G \pm 176.28 M |
| Flado | 86.98% \pm 0.11% | -5.93 P \pm 15.08 T | -69.17 G \pm 176.28 M |

Flado is highly elastic under different system heterogeneity levels.

Thanks

