# Difficulty-based Sampling for Debiased Contrastive Representation Learning

Taeuk Jang<sup>1</sup>

Xiaoqian Wang<sup>1</sup>

CVPR 2023

Poster Tag: THU-PM-328



Purdue University<sup>1</sup>



## Overview

#### Motivation

- Due to unsupervised nature, it is not trivial to find *legitimate* negative samples in contrastive learning, *e.g., false negative problem*.
- Previous works proposed statistical approaches to address the problem such as false negative debiasing and hard negative mining.

#### Contributions

- Propose a novel debiased contrastive learning method that addresses the problem from a new perspective by incorporating relative difficulty with data bias.
- Introduce triplet loss as bias-amplifying contrastive loss, which serves as an effective surrogate for learning biased representation.
- Theoretically show that the triplet loss amplifies the bias in self-supervised representation learning.

# Motivation

**Contrastive Learning**<sup>[1]</sup>: Learn representation that samples with same class are gathered and different class to be apart.

- $\mathbf{x}^a \sim p(\mathbf{x})$  : anchor
- $\mathbf{x}^+ \sim p(\mathbf{x}^+ | \mathbf{x})$  : positive samples
- $\mathbf{x}^- \sim p(\mathbf{x})$  : negative samples

$$\mathbb{E}_{\mathbf{x}^{a},\mathbf{x}^{+},\mathbf{x}^{-}}\left[-\log\frac{e^{E(\mathbf{x}^{a})^{\mathsf{T}}E(\mathbf{x}^{+})}}{e^{E(\mathbf{x}^{a})^{\mathsf{T}}E(\mathbf{x}^{+})} + \sum_{j=1}^{M}e^{E(\mathbf{x}^{a})^{\mathsf{T}}E(\mathbf{x}^{-(j)})}}\right]$$

#### Finding legitimate negatives is critical

- Negative samples are drawn from the same sample space as anchor.
  - True negative vs False negative <sup>[2]</sup>: negatives can have same class as anchor.
  - Easy negative vs Hard negative <sup>[3]</sup>: hard negative samples are informative.

# Both require domain knowledge about distribution $\tau^-$ , $\tau^-$ and assume label distribution is uniform.

Ting Chen, Simon Kornblith, Mohammad Norouzi, and Geoffrey Hinton. A simple framework for contrastive learning of visual representations. In ICML, 2020.
Ching-Yao Chuang, Joshua Robinson, Lin Yen-Chen, Antonio Torralba, and Stefanie Jegelka. Debiased contrastive learning. arXiv preprint arXiv:2007.00224, 2020.
Joshua Robinson, Ching-Yao Chuang, Suvrit Sra, and Stefanie Jegelka. Contrastive learning with hard negative samples. arXiv preprint arXiv:2010.04592, 2020

# Motivation

#### Supervised Learning

- Difficulty of samples are related to data bias. For instance,
  - Texture, color, and background in image classification<sup>[1]</sup>.
  - Race and gender in face recognition<sup>[2]</sup>.
- Samples against the data bias are likely to be hard samples.
  - e.g., bird in the water vs. bird in the forest



• Emphasize bias-conflicting samples for better performance and generalization

#### as they are more informative<sup>[3,4]</sup>.

Hyojin Bahng, Sanghyuk Chun, Sangdoo Yun, Jaegul Choo, and Seong Joon Oh. Learning de-biased representations with biased representations. In ICML, 2020.
Taeuk Jang, Feng Zheng, and Xiaoqian Wang. Constructing a fair classifier with generated fair data. In AAAI, 2021

 <sup>[3]</sup> Jungsoo Lee, Eungyeup Kim, Juyoung Lee, Jihyeon Lee, and Jaegul Choo. Learning debiased representation via disentangled feature augmentation. In NeurIPS, 2021
[4] Evan Z Liu, Behzad Haghgoo, Annie S Chen, Aditi Raghunathan, Pang Wei Koh, Shiori Sagawa, Percy Liang, and Chelsea Finn. Just train twice: Improving group robustness without training group information. In ICML, 2021.



- We employ two encoders:
  - Bias-amplifying encoder E<sub>b</sub>: intentionally amplify bias that focuses on easy samples.
  - Debiased encoder  $E_d$ : emphasize hard negative samples leveraging relative difficulty by referencing representation from  $E_b$ .

Learning bias-amplifying representation



• We employ triplet loss<sup>[1]</sup> in self-supervised manner to learn bias- amplifying representation.

$$\mathcal{L}_{tri} = \mathbb{E}[||E_b(\mathbf{x}^a) - E_b(\mathbf{x}^+)||_2^2 - ||E_b(\mathbf{x}^a) - E_b(\mathbf{x}^-)||_2^2]$$

• The derivative of triplet loss for optimization:

$$\nabla_{\theta_b} \mathcal{L}_{tri} = \mathbb{E} \bigg[ 2\Delta^{+\mathsf{T}} \nabla \big( E_b(\mathbf{x}^a) - E_b(\mathbf{x}^+) \big) - 2\Delta^{-\mathsf{T}} \nabla \big( E_b(\mathbf{x}^a) - E_b(\mathbf{x}^-) \big) \bigg],$$
  
where  $\Delta^+ = E_b(\mathbf{x}^a) - E_b(\mathbf{x}^+), \quad \Delta^- = E_b(\mathbf{x}^a) - E_b(\mathbf{x}^-)$ 

[1] Florian Schroff, Dmitry Kalenichenko, and James Philbin. Facenet: A unified embedding for face recognition and clustering. In CVPR, 2015.

#### Learning bias-amplifying representation



$$\nabla_{\theta_b} \mathcal{L}_{tri} = \mathbb{E} \bigg[ 2\Delta^{+\mathsf{T}} \nabla \big( E_b(\mathbf{x}^a) - E_b(\mathbf{x}^+) \big) - 2\Delta^{-\mathsf{T}} \nabla \big( E_b(\mathbf{x}^a) - E_b(\mathbf{x}^-) \big) \bigg],$$
  
where  $\Delta^+ = E_b(\mathbf{x}^a) - E_b(\mathbf{x}^+), \quad \Delta^- = E_b(\mathbf{x}^a) - E_b(\mathbf{x}^-)$ 

> The gradient on negative sample is weighted by  $\Delta^-$ .

- > Samples distinguishable from anchor ( $\Delta^- \gg 0$ ), *i.e., easy negatives*.
- > Samples similar to anchor ( $\Delta^- \approx 0$ ), *i.e.*, hard negatives.
- Triplet loss amplifies bias in the representation.

Learning debiased representation



- We want to learn debiased encoder  $E_d$  by referencing biased encoder  $E_b$ .
- Weight each negative sample differently by relative difficulty of negative sample  $\mathbf{x}^-$  given an anchor  $\mathbf{x}^a$
- Relative difficulty:  $w((\mathbf{z}_d^a, \mathbf{z}_d^-), (\mathbf{z}_b^a, \mathbf{z}_b^-)) = 1 + \frac{\tilde{D}(\mathbf{z}^a, \mathbf{z}_d^-)}{\tilde{D}(\mathbf{z}^a, \mathbf{z}_d^-) + \tilde{D}(\mathbf{z}^a, \mathbf{z}_b^-)}$ ,

where 
$$\tilde{D}(\mathbf{z}_i^a, \mathbf{z}_i^-) = \frac{D(\mathbf{z}_i^a, \mathbf{z}_i^-)}{\max_{(\mathbf{x}^a, \mathbf{x}^-) \in \mathcal{B}} D(E_i(\mathbf{x}^a), E_i(\mathbf{x}^-))}$$

Learning debiased representation







Representation by  $E_b$ 

- $w \in [1,2]$ 
  - $w \approx 2$  (hard negatives):  $\widetilde{D}(\mathbf{z}_b^a, \mathbf{z}_b^-) \ll \widetilde{D}(\mathbf{z}_d^a, \mathbf{z}_d^-)$
  - $w \approx 1$  (easy negatives):  $\widetilde{D}(\mathbf{z}_b^a, \mathbf{z}_b^-) \gg \widetilde{D}(\mathbf{z}_d^a, \mathbf{z}_d^-)$
- Emphasize negative samples projected closer to anchor by  $E_b$  as

$$\mathbb{E}\bigg[-\log\frac{e^{E(\mathbf{x}^{a})^{\mathsf{T}}E(\mathbf{x}^{+})}}{e^{E(\mathbf{x}^{a})^{\mathsf{T}}E(\mathbf{x}^{+})}+w(\mathbf{z}^{a},\mathbf{z}_{b}^{-},\mathbf{z}_{d}^{-})e^{E(\mathbf{x}^{a})^{\mathsf{T}}E(\mathbf{x}^{-})}}\bigg]$$

• We can also apply statistical debiasing as DCL<sup>[1]</sup> and HCL<sup>[2]</sup>.

Ching-Yao Chuang, Joshua Robinson, Lin Yen-Chen, Antonio Torralba, and Stefanie Jegelka. Debiased contrastive learning. arXiv preprint arXiv:2007.00224, 2020.
Joshua Robinson, Ching-Yao Chuang, Suvrit Sra, and Stefanie Jegelka. Contrastive learning with hard negative samples. arXiv preprint arXiv:2010.04592, 2020

### Quantitative Results

		CIFAR-10			CIFAR-100		
Method	Y	ACC (top-1)	ACC (top-5)	ACC (worst)	ACC (top-1)	ACC (top-5)	ACC (worst)
JTT [26]	0	$85.67\pm0.7$	$99.65\pm0.2$	$72.33 {\pm}~0.5$	$61.66\pm0.6$	$83.53\pm0.9$	$24.00\pm1.5$
SimCLR [4]	×	$89.12\pm0.6$	$99.74\pm0.1$	$75.7\pm0.4$	$64.86\pm0.6$	$89.67\pm0.3$	$20.00\pm0.2$
DCL [ <mark>8</mark> ]	×	$91.66 \pm 0.3$	$99.78 \pm 0.1$	$81.2 {\pm} 0.2$	$68.26 \pm 0.3$	$91.19 \pm 0.1$	$20.00 \pm 0.2$
HCL [36]	×	$91.25\pm0.2$	$99.78 \pm 0.1$	$81.5 \pm 0.2$	$68.73 \pm 0.4$	$91.19 \pm 0.1$	$29.00 \pm 0.8$
WCL $(E_d)$	×	92.71±0.3	<b>99.84±0.1</b>	83.3±0.8	69.09±0.2	91.63±0.3	<b>31.00±0.7</b>
WCL $(E_b)$	×	$75.61 \pm 0.7$	$98.61\pm0.4$	$52.6\pm0.5$	$41.61 \pm 0.3$	$69.26\pm0.2$	$1.0\pm0.5$

Table 1. Performance evaluation on CIFAR-10 and CIFAR-100.

		Waterbi	rds [37]	CelebA [27]		
Method	Y	ACC (top-1)	ACC (worst)	ACC (top-1)	ACC (worst)	
JTT [26]	0	$77.81 \pm 2.3$	$70.00\pm1.5$	$76.83{\pm}1.3$	$67.66\pm0.5$	
SimCLR [4]	×	$77.80 \pm 1.5$	0.00	$78.61 \pm 1.5$	$44.30\pm0.7$	
DCL [8]	×	$65.80 \pm 1.7$	$4.51\pm1.2$	$77.12 \pm 1.6$	$44.95\pm0.3$	
HCL [36]	×	$69.31 \pm 1.2$	$5.26\pm1.1$	$76.13\pm2.1$	$52.13\pm0.8$	
WCL $(E_d)$	×	$76.92\pm0.3$	$\textbf{31.58} \pm \textbf{3.5}$	$78.11\pm2.3$	$\textbf{57.40} \pm \textbf{1.2}$	
WCL $(E_b)$	×	$73.64 \pm 1.4$	$14.29\pm1.5$	$58.84 \pm 2.5$	$39.79 \pm 1.3$	

Table 2. Performance evaluation on Waterbirds and CelebA dataset. Note thet JTT is supervised learning method. Among the self-supervised learning methods, WCL (ours) achieves the best worst group accuracy with comparable overall performance.

# Qualitative Results



• Visualization of top-5 easy/hard negative on CUB dataset



(a) Top-5 easy negatives



(b) Top-5 hard negatives

#### Thank you for watching and see you by our poster

Difficulty-based Sampling for Debiased Contrastive Representation Learning

Poster Tag: THU-PM-328

Taeuk Jang<sup>1</sup>

Xiaoqian Wang<sup>1</sup>



Purdue University<sup>1</sup>

