

# Learning Federated Visual Prompt in Null Space for MRI Reconstruction

Chun-Mei Feng<sup>1</sup>, Bangjun Li<sup>2</sup>, Xinxing Xu<sup>1</sup>, Yong Liu<sup>1</sup>, Huazhu Fu<sup>1</sup>, Wangmeng Zuo<sup>3</sup>

<sup>1</sup>Institute of High Performance Computing (IHPC), Agency for Science, Technology and Research (A\*STAR), Singapore;

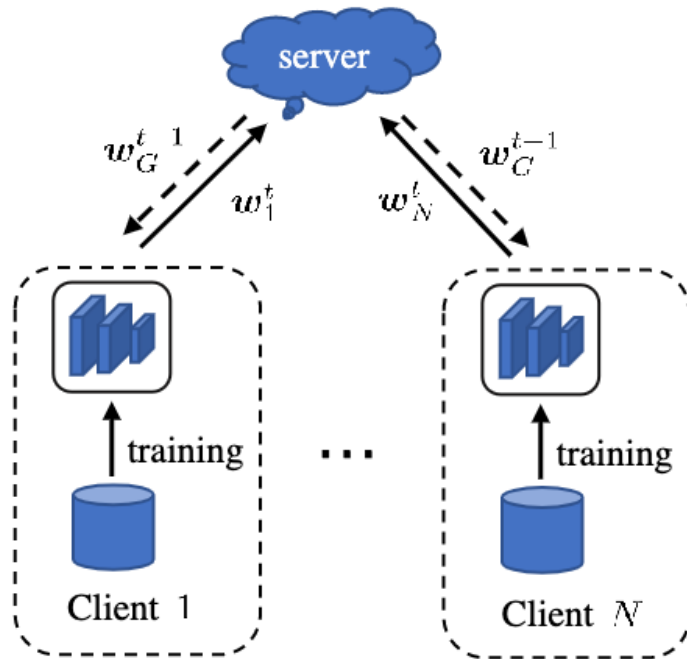
<sup>2</sup>Shangdong University, China;

<sup>3</sup>Harbin Institute of Technology, Harbin, China;

strawberry.feng0304@gmail.com;

<https://github.com/chunmeifeng/FedPR>

## What is the federated learning?



**Goals:** To facilitate multi-institutional collaborations between data centers. Allowing **collaborative and decentralized training** of deep learning-based methods.

A classical FL method, **FedAvg**, **first** receives global model parameters from the server and initializes the client model parameters. **Then**, each client trains model locally on private data and sends the local model to the server. **Finally**, the server aggregates the local updates and further updates the global model by averaging the parameters which will be **sent back** to each client **in the next round**.

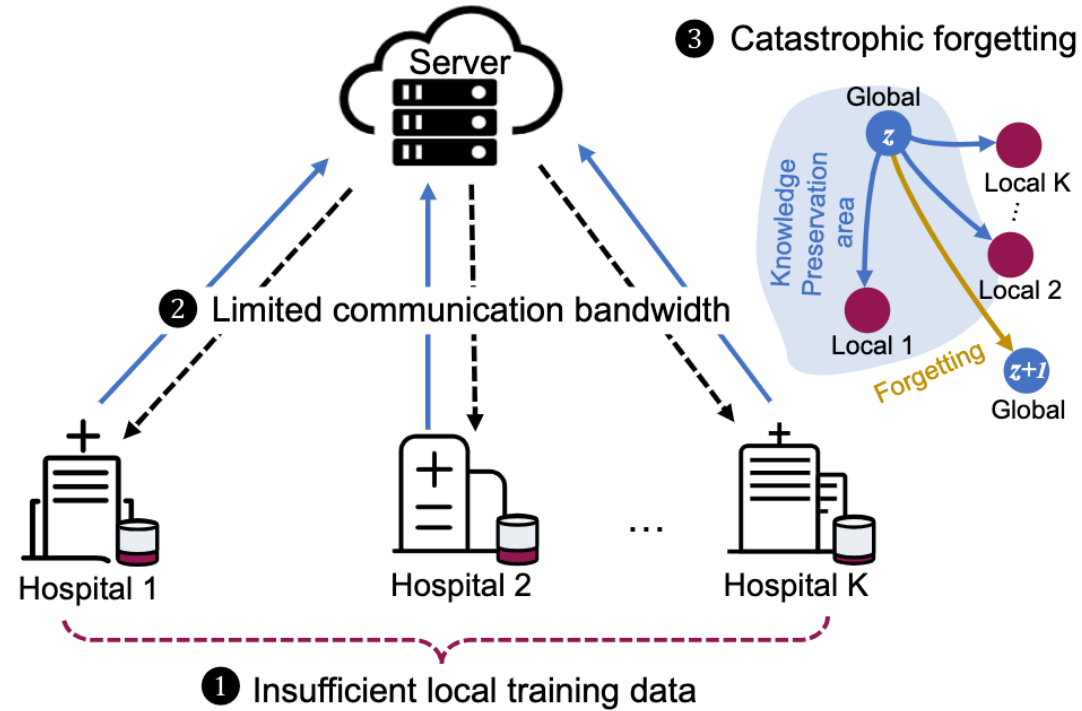
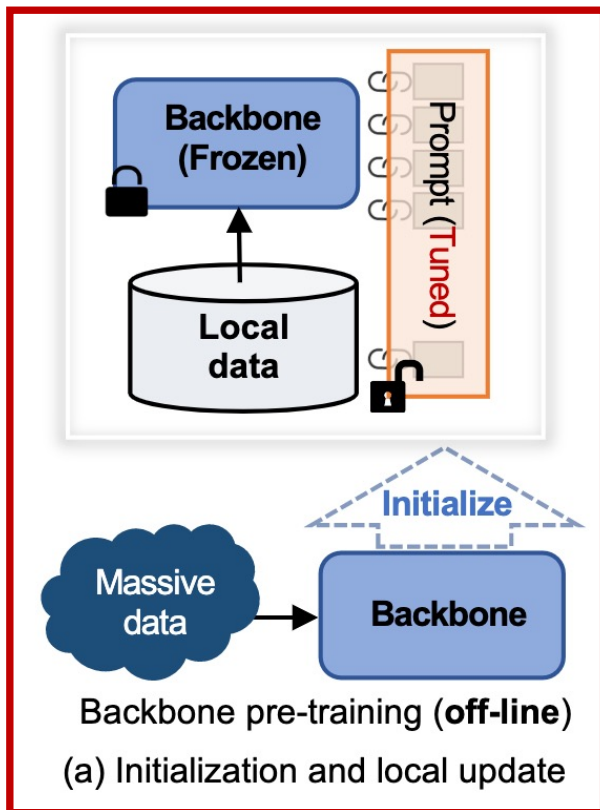


Figure 1. **Illustration** of the three **key issues** in federated MRI.

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## 1 Insufficient local training data



## 2 Limited communication bandwidth

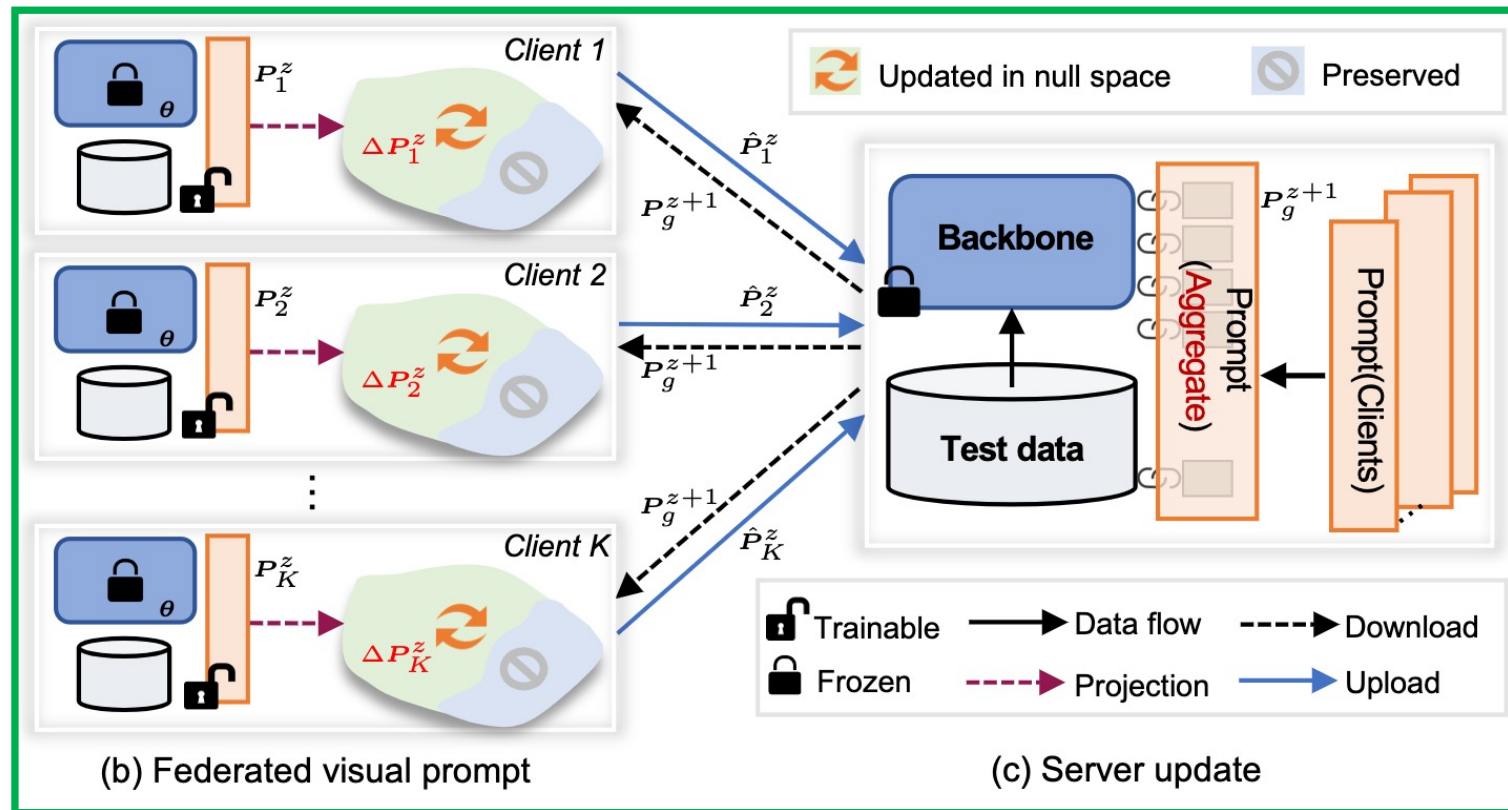


Figure 2. **Illustration** of our **FedPR** method. (a) For each client, the backbone model is pre-trained on massive data and fine-tuned via prompt (see Sec. 3.2). (b) *Federated visual prompt* is executed by updating the local prompt of each client only in the approximate null space of global prompts while preserving the *previously* acquired global knowledge (see Sec. 3.3). (c) Server update by aggregating local prompts.

3 Catastrophic forgetting

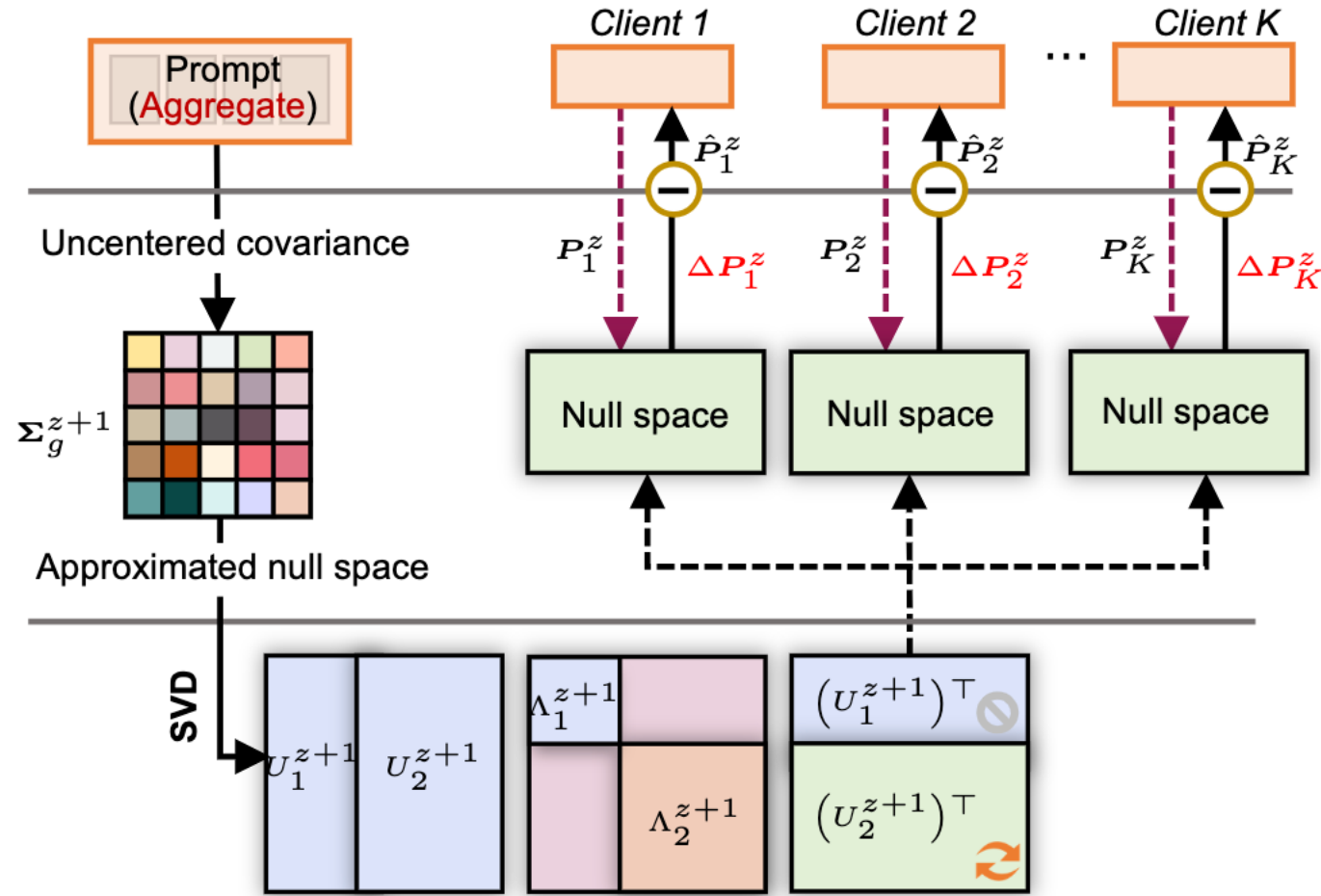


Figure 3. **Illustration of federated visual prompt** for updating local prompts in the null space of global prompts.

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**Algorithm 1: FedPR**

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**Input:** Private datasets from  $K$  clients:  
 $\mathcal{D}^1, \mathcal{D}^2, \dots, \mathcal{D}^K$ , local updates  $T$ ,  
communication rounds  $Z$ , pre-trained model  
parameters  $\theta$ , prompt embeddings  $P$ ,  
learning rate  $\eta$ , hyperparameter  $\gamma$ ;

```
1 // ServerExecution:
2 Initialize global prompt  $P_g$  with parameters  $\theta$ .
3 for each communication round  $z \in \{1, 2, \dots, Z\}$  do
4   for each client  $k \in \{1, 2, \dots, K\}$  in parallel do
5      $P_k^z \leftarrow P_g^z$ ;
6      $\hat{P}_k^z \leftarrow \text{LocalUpdate}(k, P_k^z)$ ;
7   end
8    $P_g^{z+1} \leftarrow \sum_{k=1}^K \frac{|\mathcal{D}^k|}{|\mathcal{D}|} \hat{P}_k^z$ ;
9   Compute the uncentered covariance matrix:
10   $\Sigma_g^{z+1} = (P_g^{z+1})^\top P_g^{z+1}$ ;
11  Approximate the null space of  $\Sigma_g^{z+1}$ :
12   $\Sigma_g^{z+1} = U^{z+1} \Lambda^{z+1} (U^{z+1})^\top$ ;
13  Select the smallest diagonal singular values of
14   $\Lambda_2^{z+1}$  with the ratio of  $\gamma$ ;
15  Get  $U_2^{z+1}$  corresponding to  $\Lambda_2^{z+1}$ .
16 end
17 return  $P_g^{z+1}$ 
18 // LocalUpdate ( $k, P_k$ ):
19 for each local epoch  $t \in \{1, 2, \dots, T\}$  do
20   Get the updated parameters  $\Delta P_k^z$ :
21    $\Delta P_k^z = U_2^{z+1} (U_2^{z+1})^\top P_k^z$ ;
22    $\hat{P}_k^{z,t+1} \leftarrow P_k^{z,t} - \eta_k \Delta P_k^{z,t}$ ;
23 end
24 return  $\hat{P}_k^z$ 
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Table 1. **Quantitative comparison** of state-of-the-art FL methods with regard to In-Federation and Out-of-Federation scenarios, where # **Com.cost** is the communication cost, Ub indicates the upper-bound of FL algorithms,  $\uparrow$  and  $\downarrow$  indicate increments and decrements compared with FedAvg (w. FFt). Detailed analyses are provided in Sec. 4.2.

Method	# Com.cost	In-Federation			Out-of-Federation		
		PSNR	SSIM	NMSE	PSNR	SSIM	NMSE
SingleSet	18.43 M	28.79(3.35) $\downarrow$	0.805(0.099) $\downarrow$	0.021(0.011) $\downarrow$	28.92(2.15) $\downarrow$	0.808(0.091) $\downarrow$	0.032(0.011) $\downarrow$
Centralized (Ub)	18.43 M	36.71(4.57) $\uparrow$	0.947(0.044) $\uparrow$	0.009(0.005) $\uparrow$	35.73(4.66) $\uparrow$	0.940(0.041) $\uparrow$	0.008(0.013) $\uparrow$
FedAvg (w. FFt) [22]	18.43 M	32.14(0.00)	0.903(0.000)	0.010(0.000)	31.07(0.00)	0.899(0.000)	0.021(0.000)
FedBN [18]	18.69 M	28.31(3.83) $\downarrow$	0.817(0.086) $\downarrow$	0.044(0.034) $\downarrow$	25.65(5.42) $\downarrow$	0.731(0.186) $\downarrow$	0.080(0.059) $\downarrow$
FedProx [17]	18.43 M	32.84(0.70) $\uparrow$	0.901(0.002) $\uparrow$	0.010(0.000)	31.98(0.91) $\uparrow$	0.905(0.006) $\uparrow$	0.018(0.003) $\uparrow$
SCAFFOLD [12]	18.43 M	33.08(0.94) $\uparrow$	0.914(0.010) $\uparrow$	0.009(0.001) $\uparrow$	32.20(1.13) $\uparrow$	0.915(0.016) $\uparrow$	0.018(0.003) $\uparrow$
MOON [16]	18.43 M	34.06(1.92) $\uparrow$	0.927(0.023) $\uparrow$	0.008(0.002) $\uparrow$	31.16(0.09) $\uparrow$	0.907(0.008) $\uparrow$	0.023(0.002) $\downarrow$
FedReg [35]	18.43 M	33.29(1.15) $\uparrow$	0.890(0.013) $\uparrow$	0.009(0.001) $\uparrow$	32.41(1.34) $\uparrow$	0.907(0.008) $\uparrow$	0.017(0.004) $\uparrow$
FL-MRCM [9]	18.43 M	33.60(1.46) $\uparrow$	0.922(0.019) $\uparrow$	0.013(0.003) $\downarrow$	32.72(1.65) $\uparrow$	0.911(0.012) $\uparrow$	0.016(0.005) $\uparrow$
FedMRI [7]	17.46 M	33.35(1.21) $\uparrow$	0.923(0.020) $\uparrow$	0.014(0.004) $\downarrow$	32.00(0.93) $\uparrow$	0.914(0.015) $\uparrow$	0.019(0.002) $\uparrow$
<b>Ours (w. Pro)</b>	<b>0.11 M</b>	<b>35.29(3.15) <math>\uparrow</math></b>	<b>0.927(0.024) <math>\uparrow</math></b>	<b>0.009(0.001) <math>\uparrow</math></b>	<b>34.65(3.58) <math>\uparrow</math></b>	<b>0.921(0.022) <math>\uparrow</math></b>	<b>0.010(0.011) <math>\uparrow</math></b>
<b>Ours (Full)</b>	<b>0.11 M</b>	<b>36.43(4.30) <math>\uparrow</math></b>	<b>0.945(0.042) <math>\uparrow</math></b>	<b>0.007(0.003) <math>\uparrow</math></b>	<b>35.60(4.53) <math>\uparrow</math></b>	<b>0.939(0.040) <math>\uparrow</math></b>	<b>0.008(0.013) <math>\uparrow</math></b>

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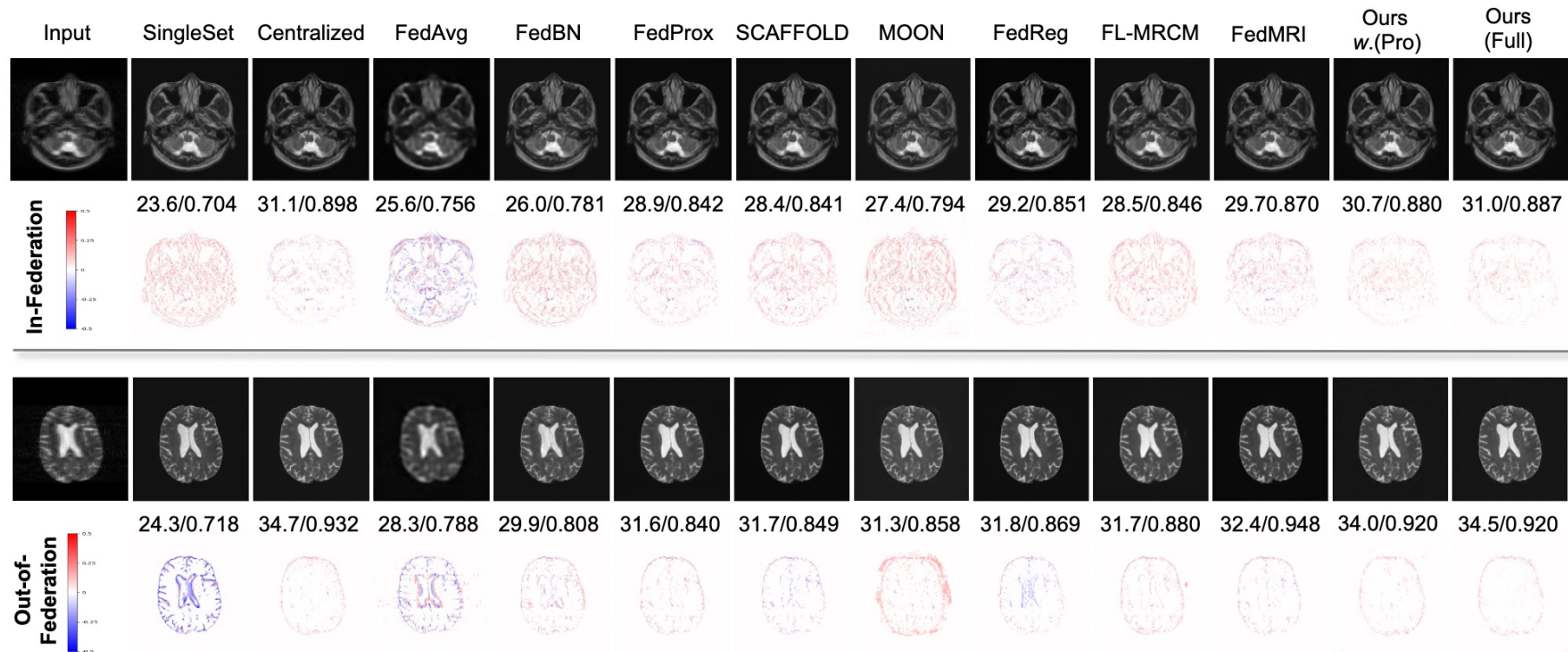
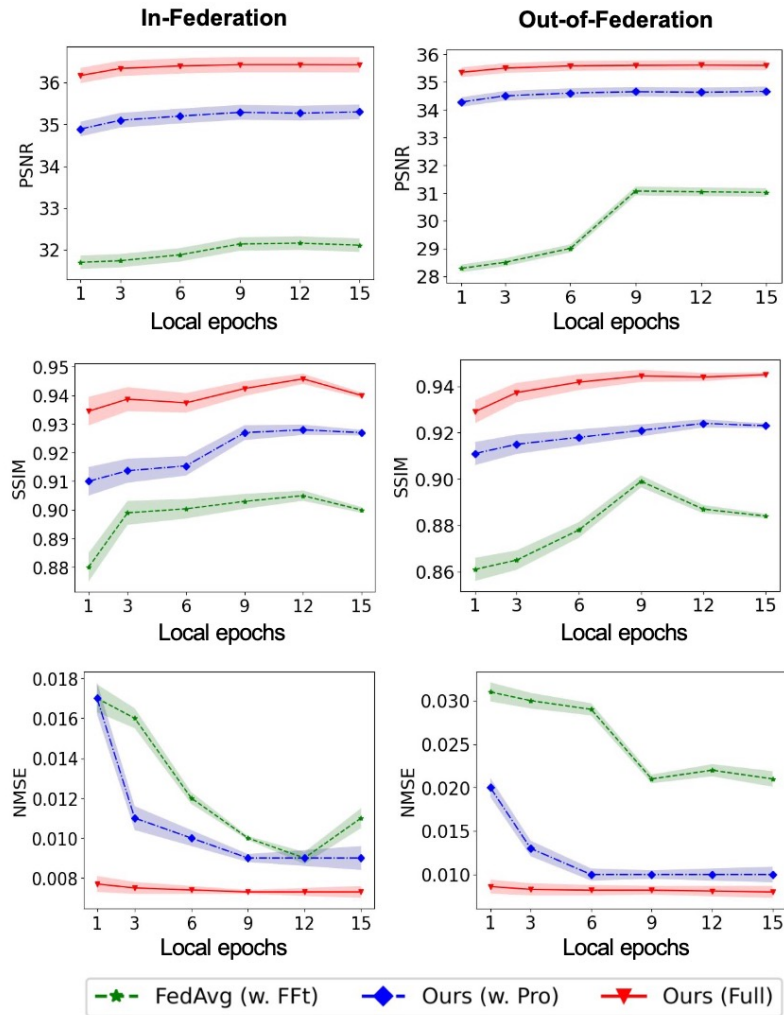


Figure 4. **Qualitative comparison** of different algorithms in terms of reconstruction images and error maps with corresponding quantitative measurements in PSNR/SSIM under In-Federation and Out-of-Federation scenarios. The less texture in the error map, the better reconstruction quality.

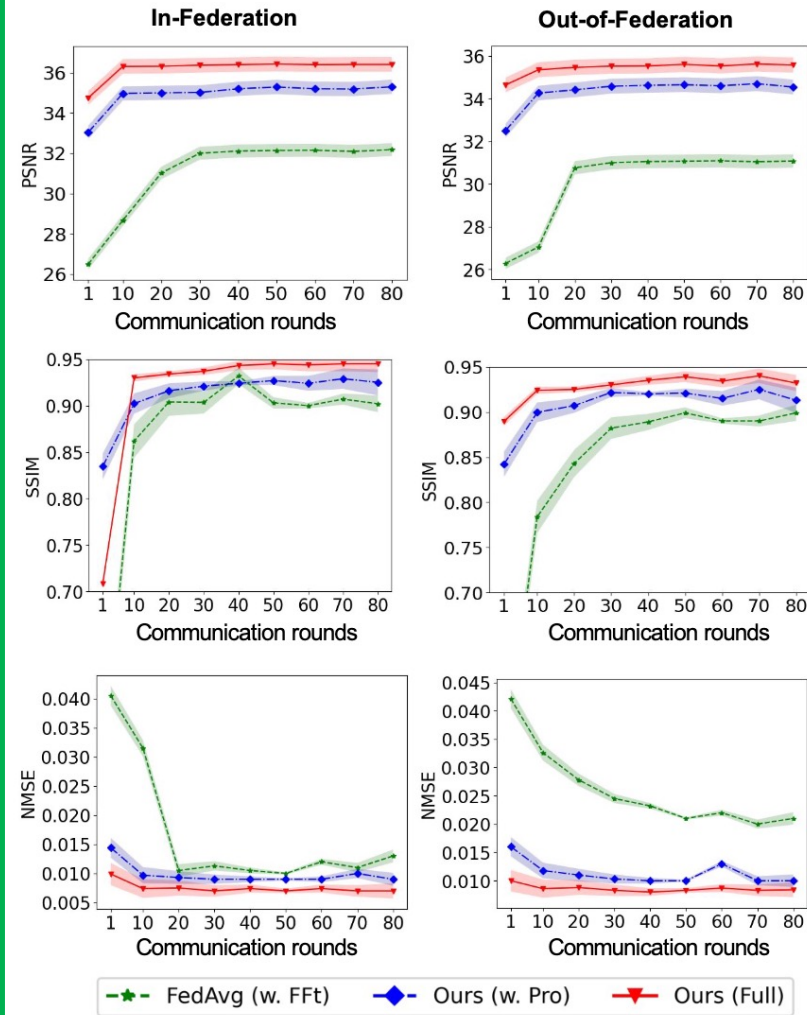


## Catastrophic Forgetting vs. Local Updates



(a)

## Communication Efficiency Analysis.



(b)

Figure 5. **Reconstruction accuracy** of FedAvg (w. FFt), **Ours** (w. Pro), and **Ours** (Full) versus (a) local epochs and (b) communication rounds under In-Federation and Out-of-Federation scenarios.

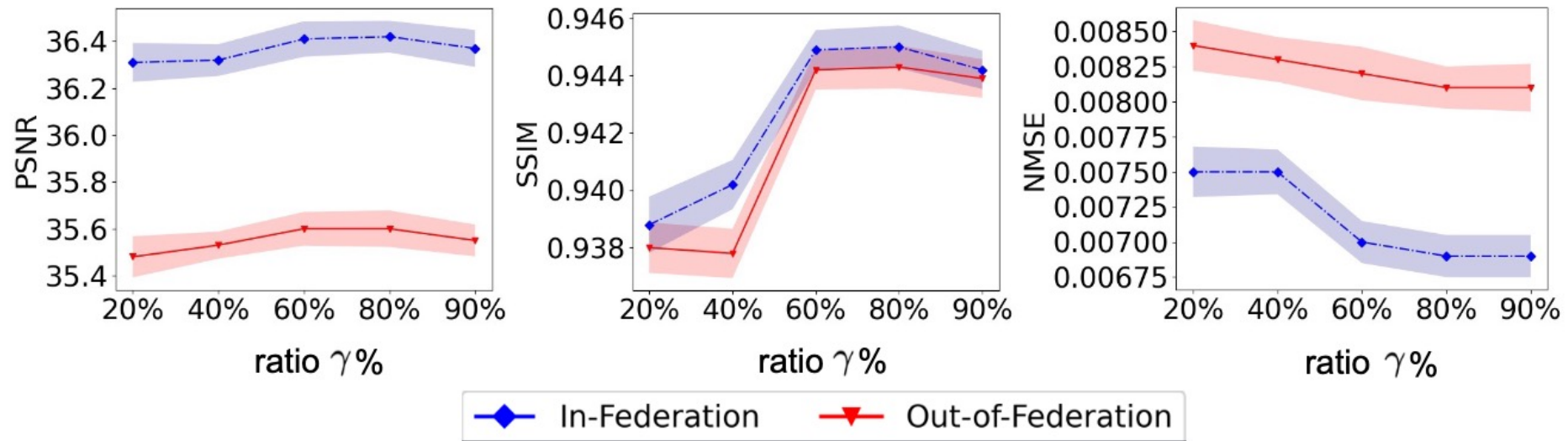


Figure 6. Analysis of the **ratio**  $\gamma\%$  of the approximate null space in terms of PSNR, SSIM, and NMSE.

*Thanks!*