

RASP: Revisiting 3D Anamorphic Art For Shadow-Guided Packing of Irregular Objects



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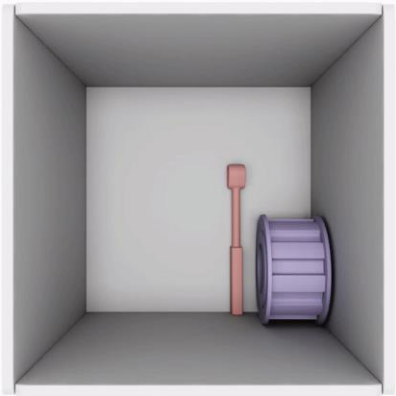


Shanmuganathan Raman
CVIG Lab, IIT Gandhinagar

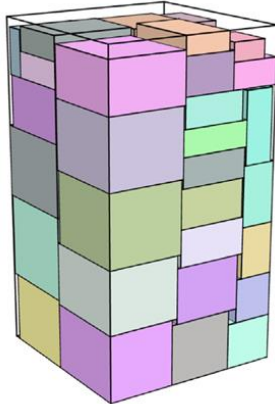


Background

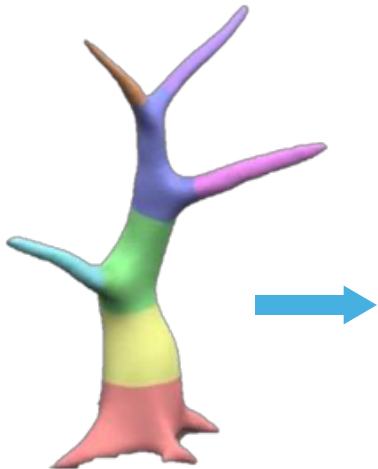
3D Packing Problems



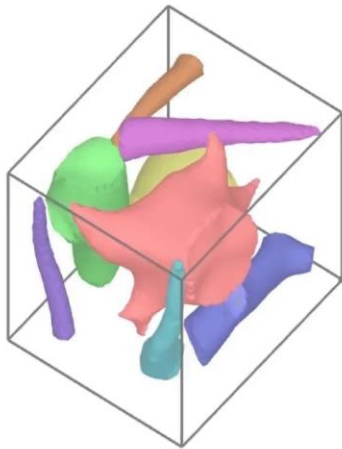
First person view of packing



A well packed container



A 3D Model



Packing the parts into a box

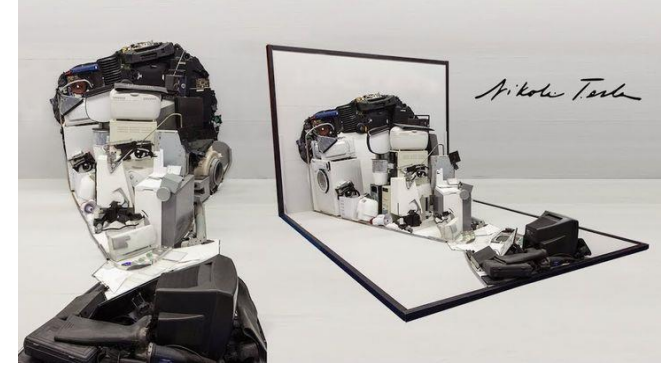
Shadow Art and 3D Anamorphic Art



Sunset over Manhattan

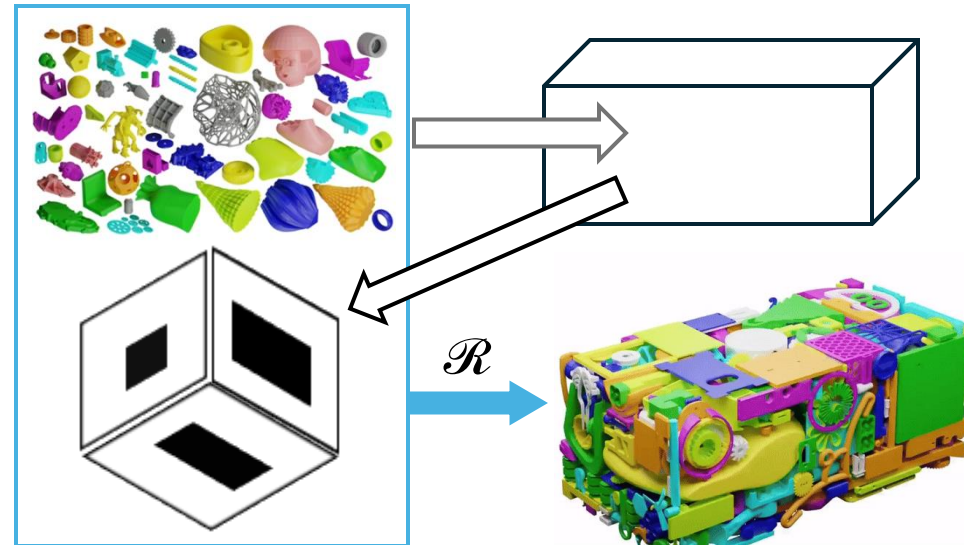


Wild mood swings



Portrait of Nikola Tesla using appliances

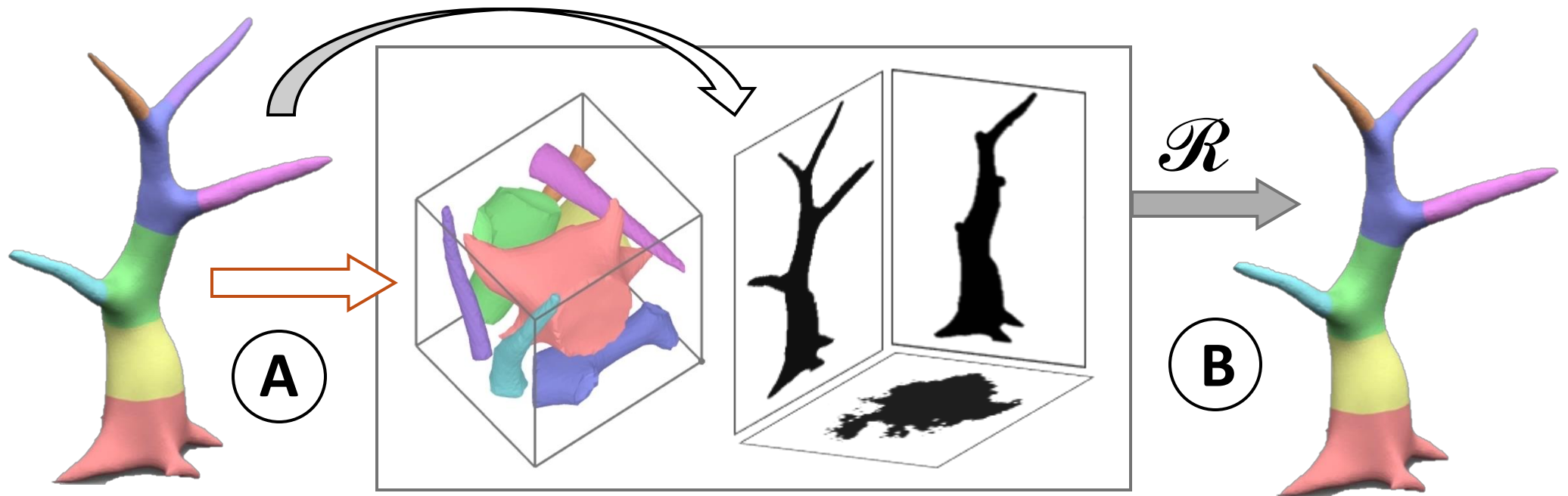
Shadow Guided 3D Packing



Dual Interpretation of the Problem

Ⓐ 3D Packing Problem

Ⓑ 3D Part Assembly



Existing Research

3D Packing Problem

● Classical Algorithms

Ocloo et al. [2020], Paquay et al. [2016]

Formulates as Mixed Integer Linear Programming.
Receive an optimal solution **but cannot address large object numbers.**

● Heuristic Algorithms

Gürbüz et al. [2009] Largest Area First-Fit (LAFF).

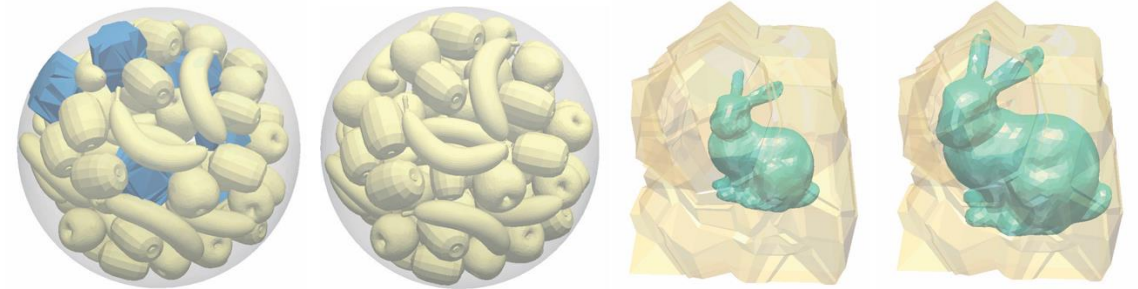
Toffolo et al. [2017] Two level stacks-based method.
Shorter time **but low-quality solutions.**

● Meta-Heuristic Algorithms

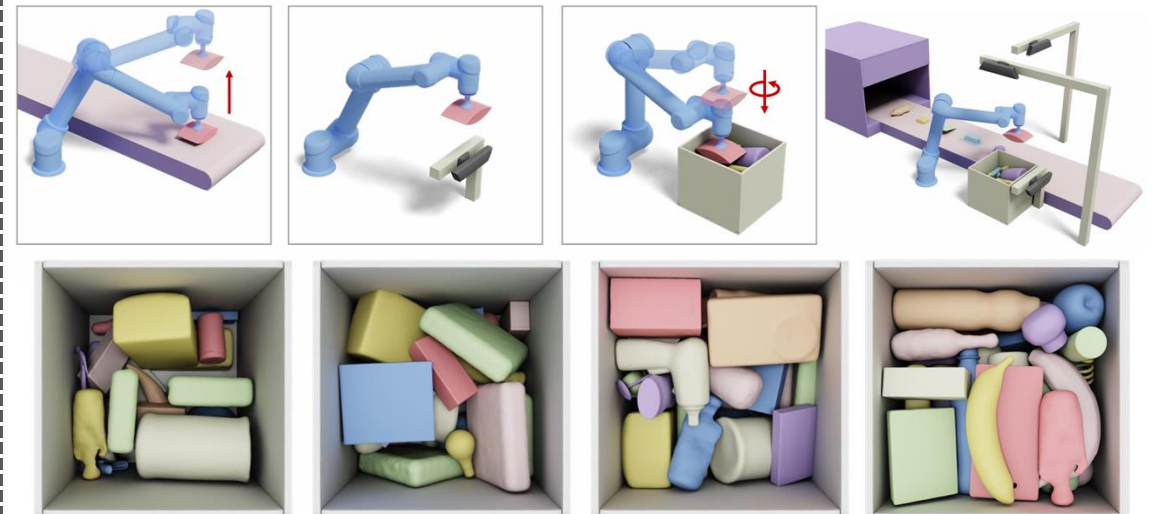
Xiang et al. [2018], Li et al. [2014]

Genetic Algorithm and Greedy based solution.
High-quality approximate **solutions but search process is time-consuming.**

Packing Irregular Objects in 3d Space via Hybrid Optimization, Ma et al. [2018]

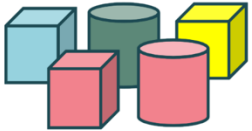


Learning Physically Realizable Skills for Online Packing of General 3d Shapes, Zhao et al. [2023]



Methodology

Source Meshes \mathcal{S}

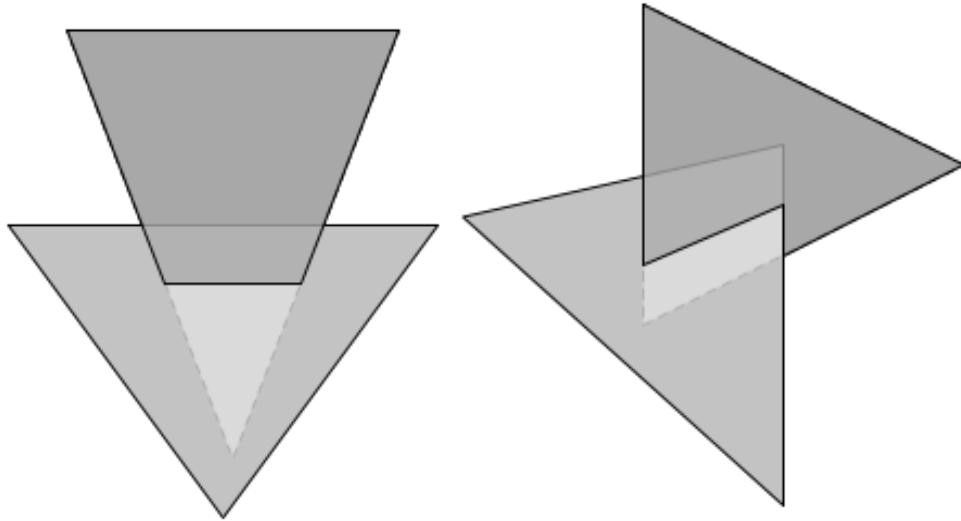


Methodology

Traditional Methods of Identifying Mesh Intersection in 3D

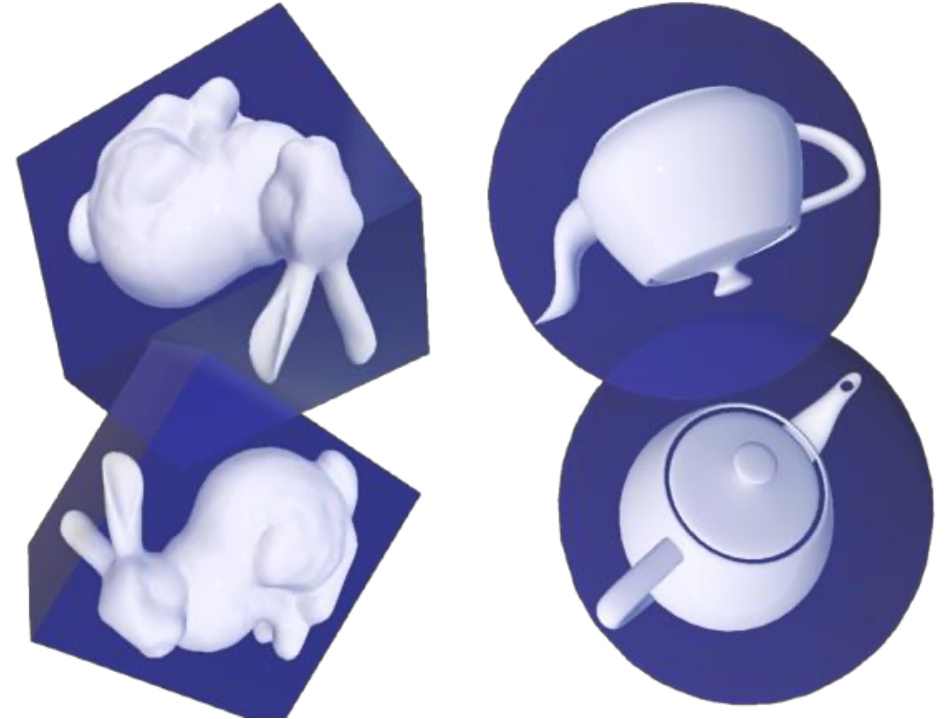
→ Triangular Face Based

Heavy in terms of compute.



→ Bounding Based

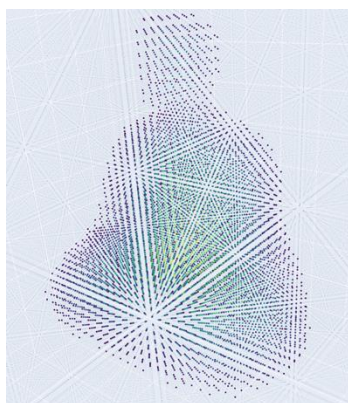
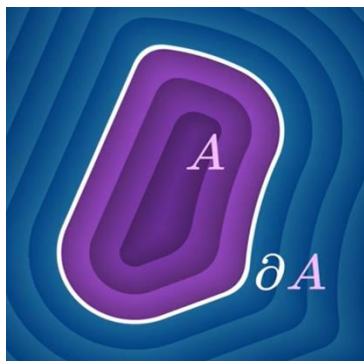
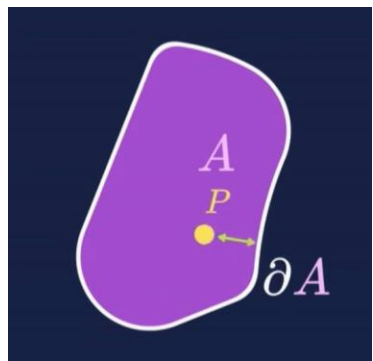
Prone to false positives.



Methodology

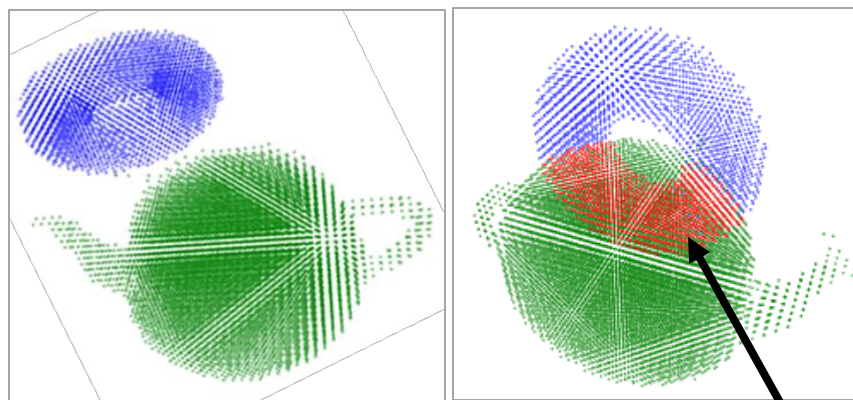
Signed Distance Function for Finding Mesh Intersection

$$d_A(P) := \begin{cases} \text{dist}(P, \partial A), & P \text{ outside} \\ -\text{dist}(P, \partial A), & P \text{ inside} \end{cases}$$



We precompute the SDF of each mesh at a fixed set of query points in the bounding volume \mathcal{V}

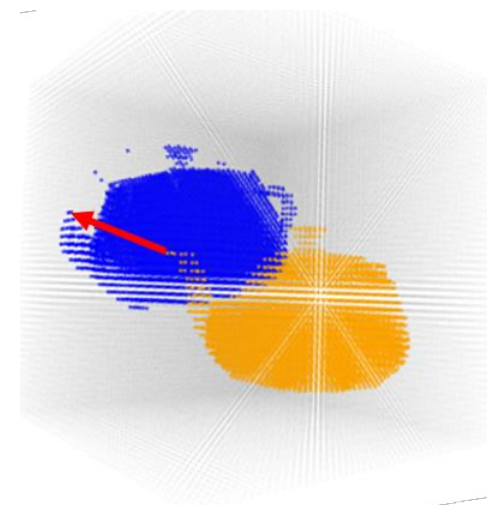
Finding the intersections is now simply counting the points for which the SDF values are less than zero with respect to more than one objects in \mathcal{V}



Intersections

We do not need to compute the SDF(s) in every iteration.

We warp the previous SDF to the new SDF through a linear transformation of the learned rotation and translations.



Methodology

Silhouette Loss

$$\mathcal{L}_{sil} = \frac{1}{MNK} \sum_{k=1}^K \sum_{i=1}^{MN} \|I_k(i) - \hat{I}_k(i)\|_2^2$$

Intersection Loss

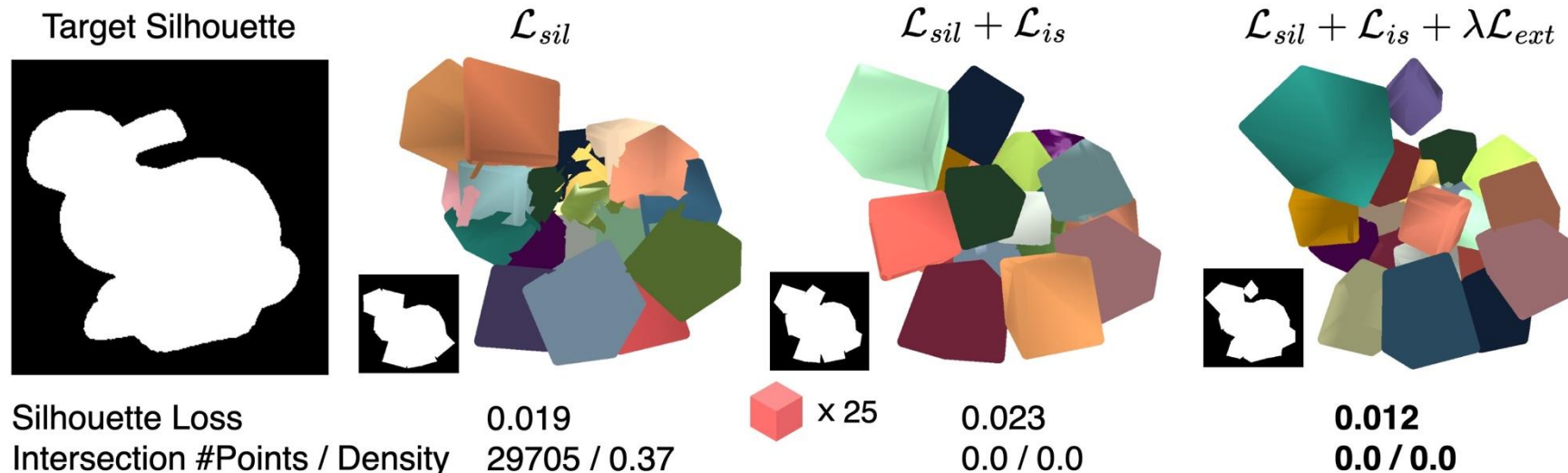
$$\mathcal{L}_{is} = \sum_{\mathbf{p} \in \mathcal{C}_p} D_{is}(\mathbf{p}) \quad D_{is}(\mathbf{p}) = \sum_{\{\forall O_i | \tilde{S}_{O_i}(\mathbf{p}) < 0\}} -\tilde{S}_{O_i}(\mathbf{p})$$

Container Extrusion Loss






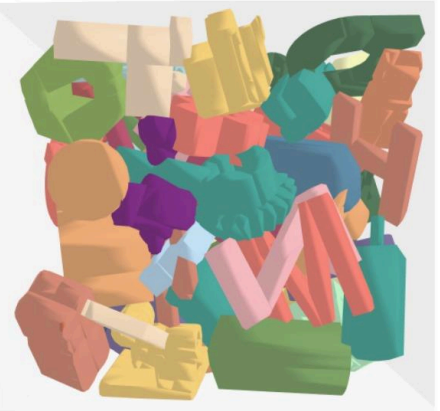


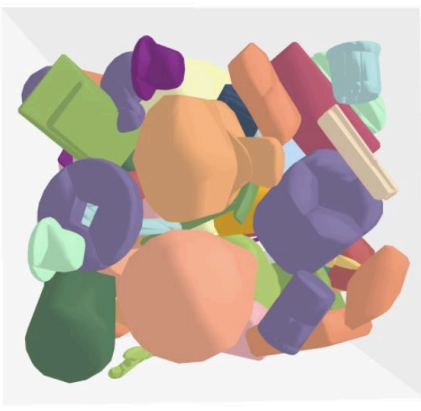

$$\mathcal{L}_{ext} = \sum_{i=1}^N \sum_{\mathbf{v} \in V_i} \max(-\epsilon, S_C(\mathbf{v}))$$

Total Loss

$$\mathcal{L}_{total} = \mathcal{L}_{sil} + \mathcal{L}_{is} + \lambda \mathcal{L}_{ext} \quad \lambda = 0.001$$

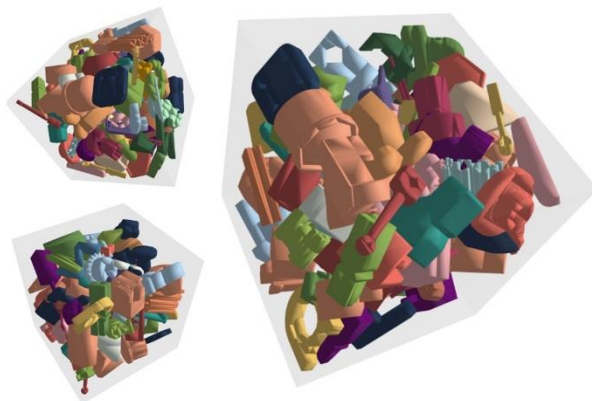


Packing Results on IR-BPP Dataset

	ABC #90	Blockout #28	Cube #24	General #67	Kitchen #120
Zhao et al.					
	PD 38.93%	PD 56.84%	PD 47.57%	PD 38.95%	PD 49.98%
RASP (ours)					
	PD 39.81%	PD 57.55%	PD 47.61%	PD 39.37%	PD 50.98%

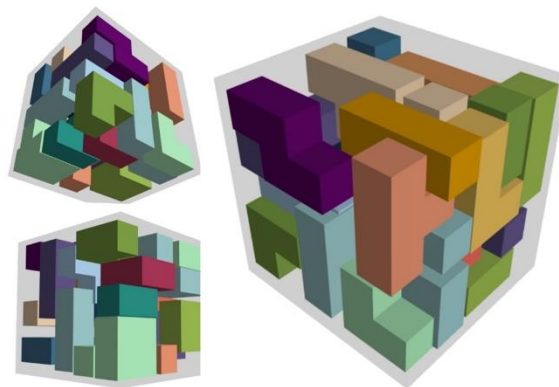
Packing Results

ABC



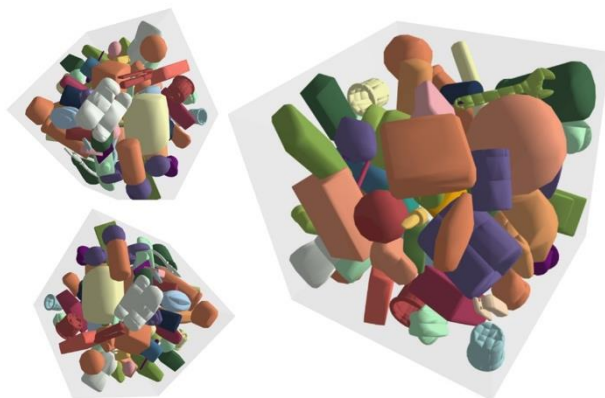
Number of Objects: **90**
Packing Density: **40%**

Block Out



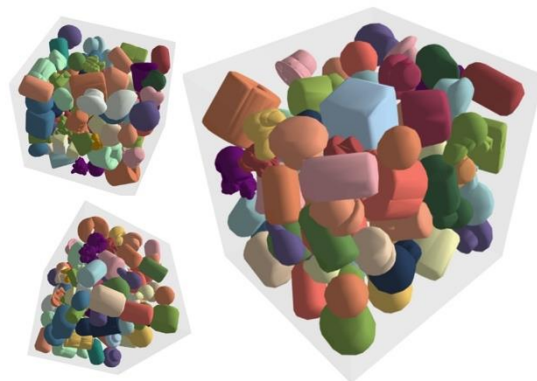
Number of Objects: **28**
Packing Density: **57%**

General

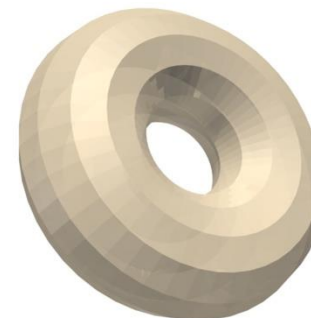


Number of Objects: **67**
Packing Density: **40%**

Kitchen



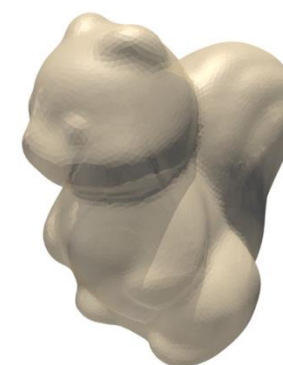
Number of Objects: **120**
Packing Density: **50%**



Number of Objects: **550**



Packing Density: **58%**

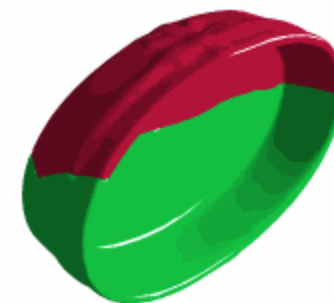
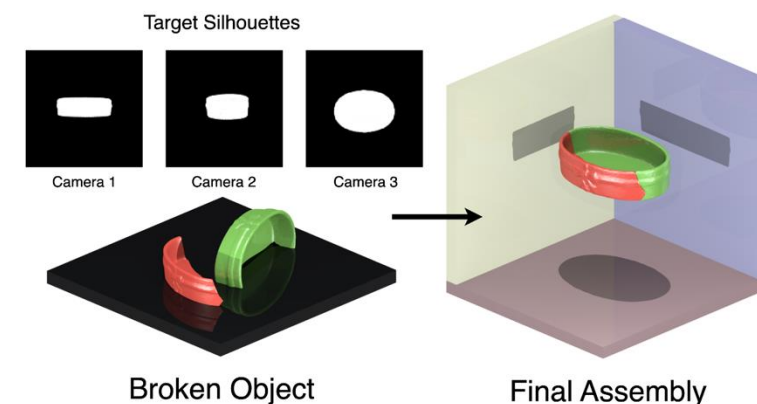
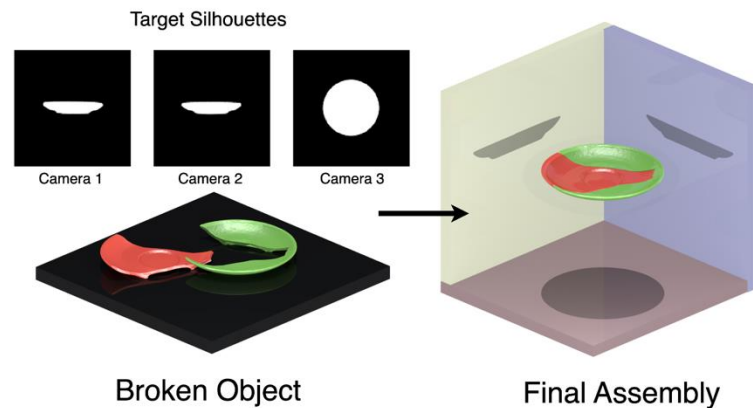
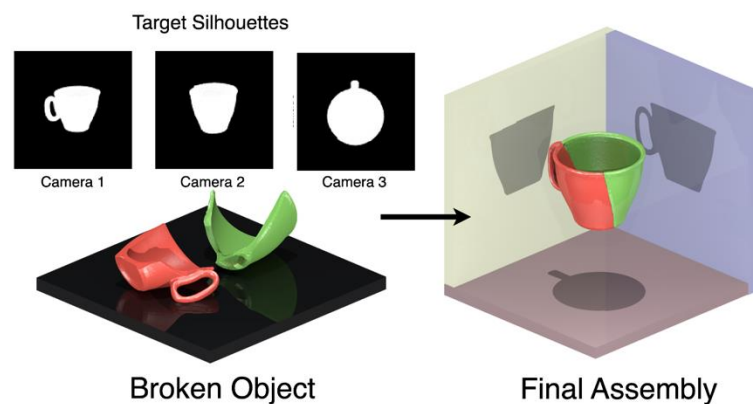


Number of Objects: **115**

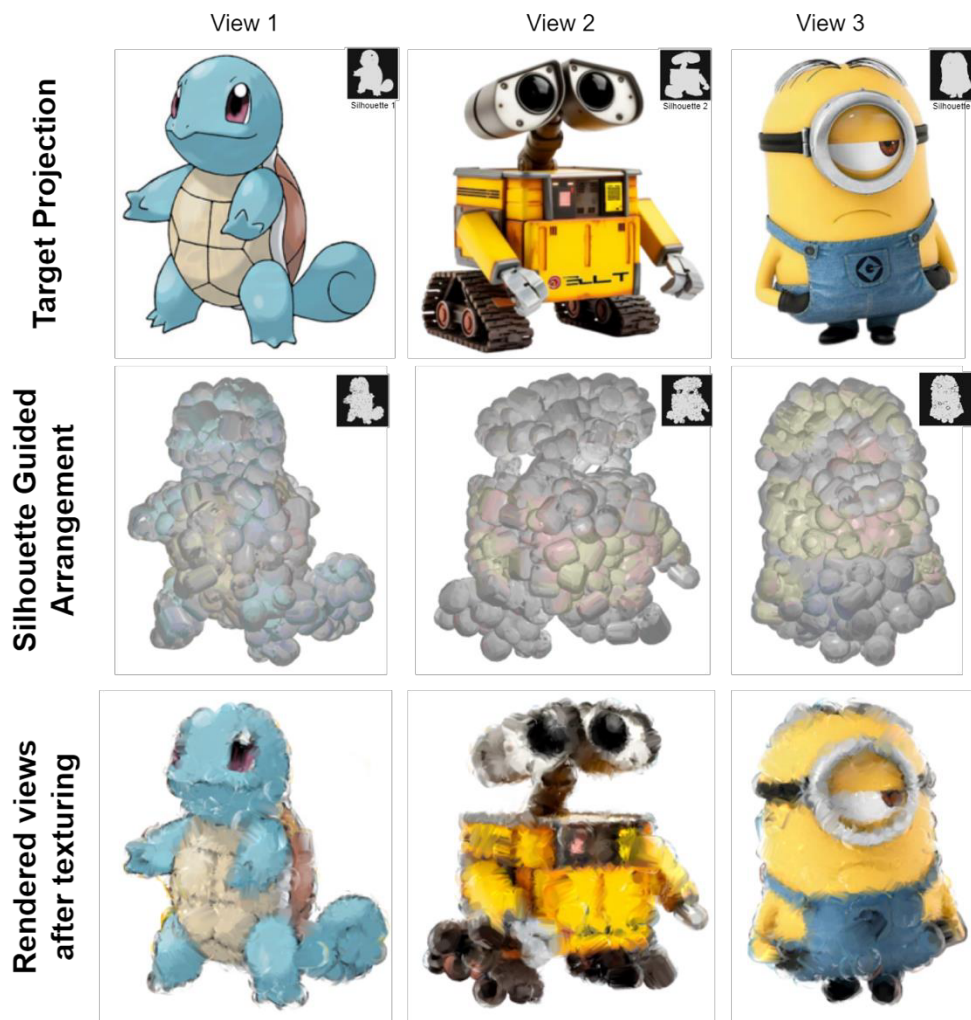


Packing Density: **34%**

3D Part Assembly Results on the Fantastic Breaks Dataset



3D Anamorphic Art

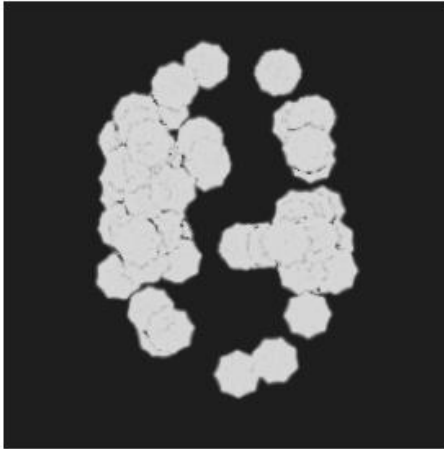


Combined MSE: **0.038**

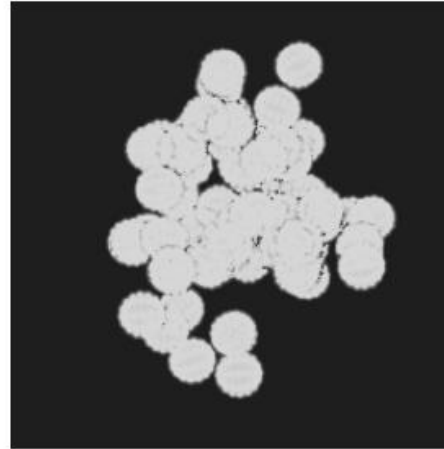


3D Anamorphic Art

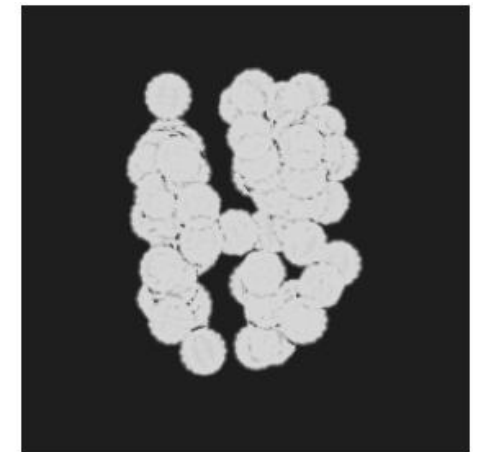
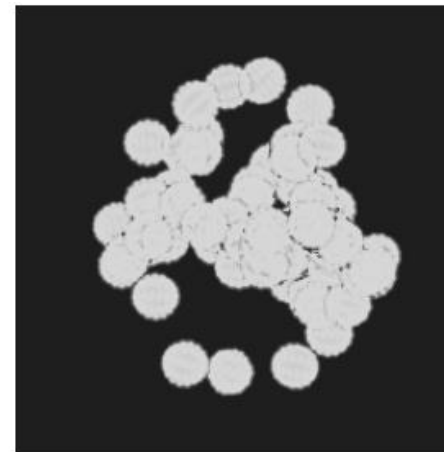
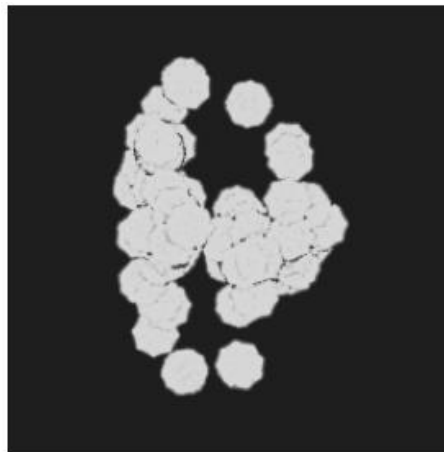
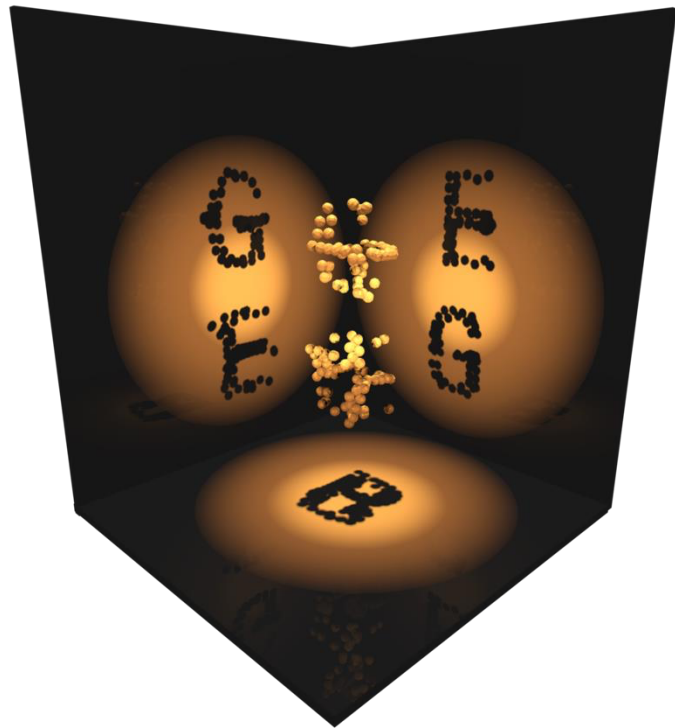
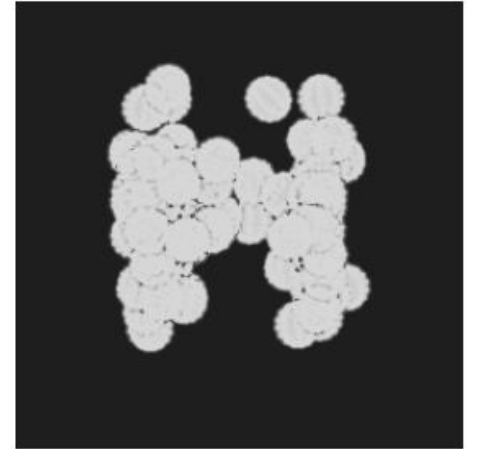
View 1



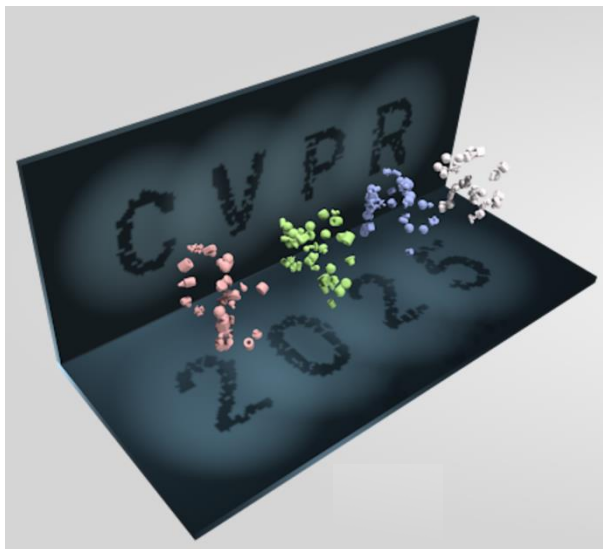
View 2



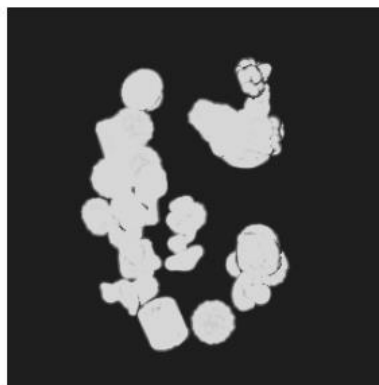
View 3



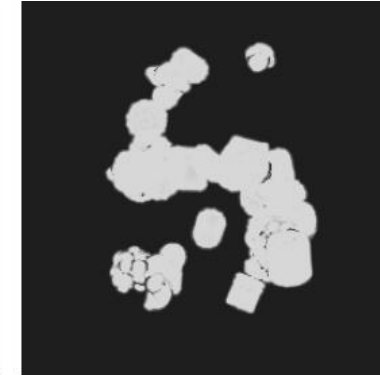
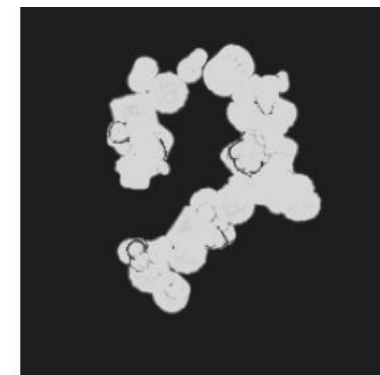
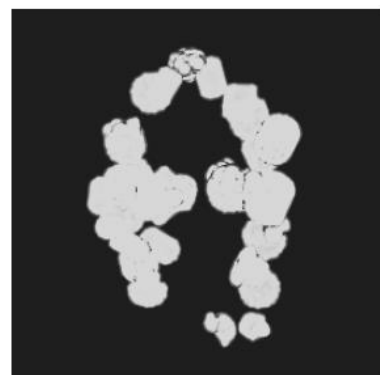
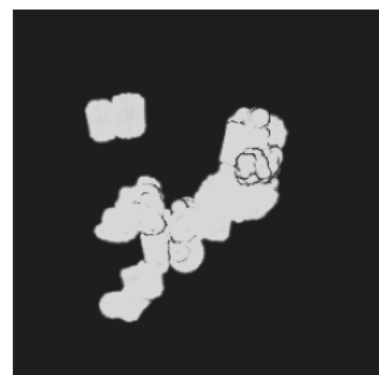
3D Anamorphic Art



View 2



View 1



Contributions

We propose a differentiable rendering-based framework to tackle irregular object packing by drawing inspiration from 3D Anamorphic Art.

We present a novel SDF-based approach to manage inter-object intersections and object-container extrusions, enhanced by an image-based loss function.

We demonstrate that RASP can also be applied to part assembly without the need for explicit 3D ground truth supervision.

We illustrate compelling visual effects that cater to multi-view anamorphic art.

To the best of our knowledge, this is the first approach to address packing (and part assembly) using only shadows or projections, guided by the principles of differentiable rendering.

References

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3. Ma, Yuexin, et al. "Packing irregular objects in 3D space via hybrid optimization." *Computer graphics forum*. Vol. 37. No. 5. 2018.
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9. Li, Xueping, Zhaoxia Zhao, and Kaike Zhang. "A genetic algorithm for the three-dimensional bin packing problem with heterogeneous bins." *IIE Annual Conference. Proceedings. Institute of Industrial and Systems Engineers (IISE)*, 2014.

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