

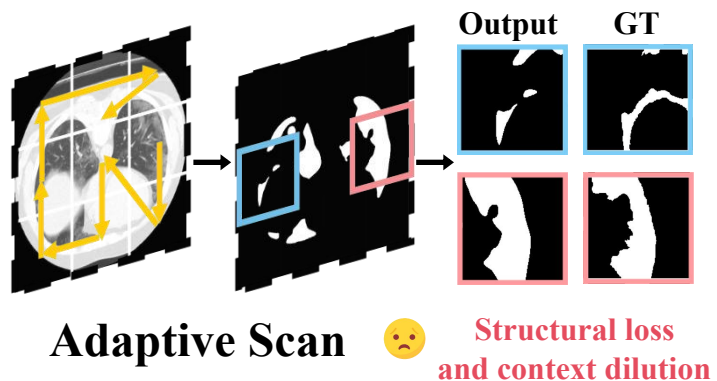
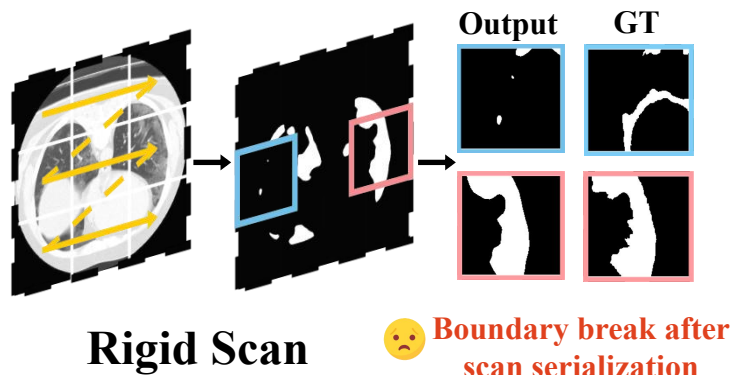
# GeoSemba

## Reconstructing State Space Model for Cross Paradigm Representation in Medical Image Segmentation

Xutao Sun<sup>1</sup>, Jiarui Li<sup>1</sup>, Junwen Liu<sup>1</sup>, Yonggong Ren<sup>1</sup>

<sup>1</sup>School of Computer Science and Artificial Intelligence  
Liaoning Normal University

# Motivation: from scan order to interaction quality



## Limitation 1

Mamba serializes 2D images into 1D token streams. Spatially adjacent tokens in the scan may be semantically mismatched, blurring discriminative evidence.

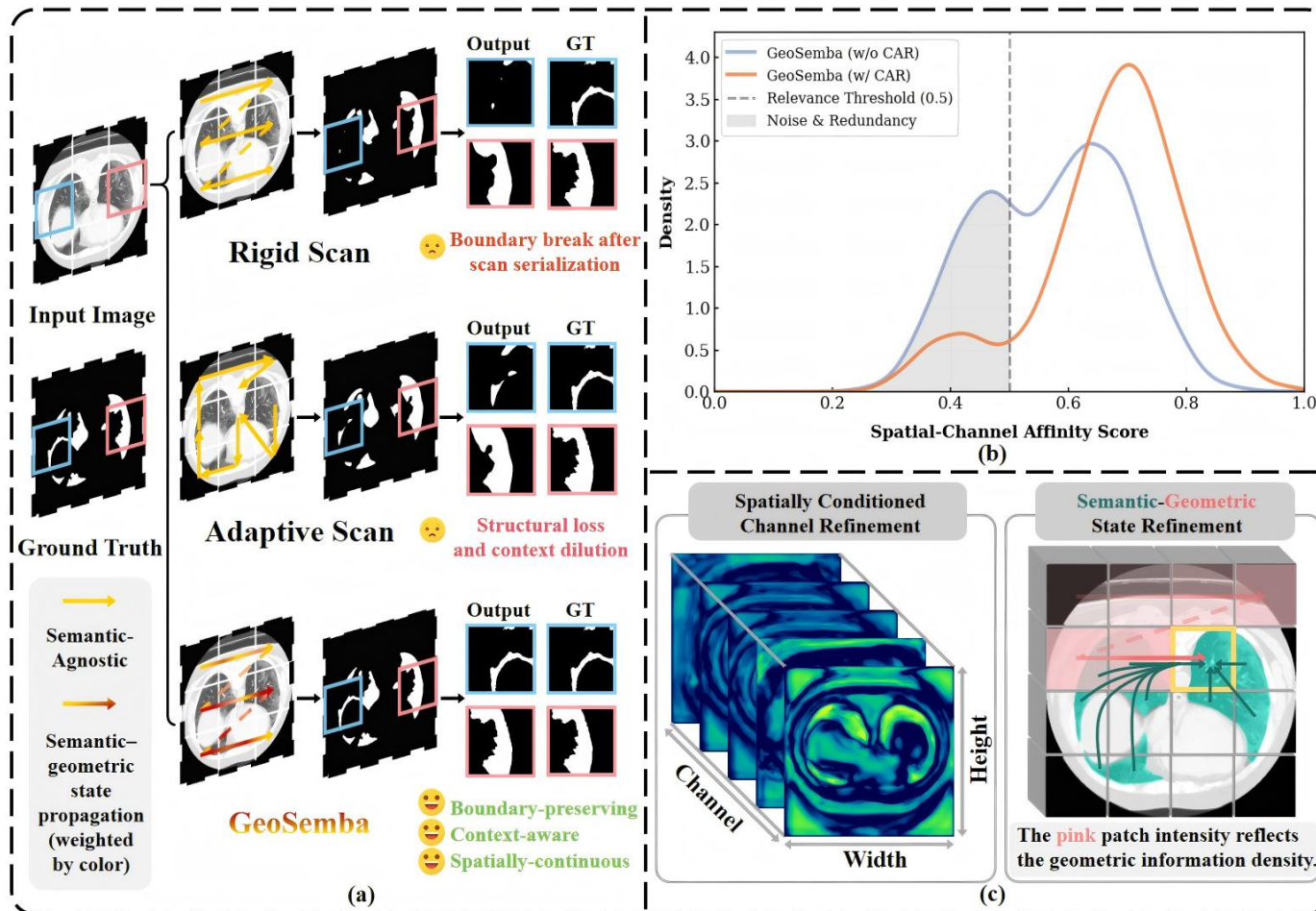
## Limitation 2

Spatial interaction and channel discrimination are often treated separately, although medical cues arise from their joint effect.

## Our question

Can a single-scan SSM preserve geometry-aware semantic propagation while modeling spatial-channel dependencies efficiently?

# Main contributions

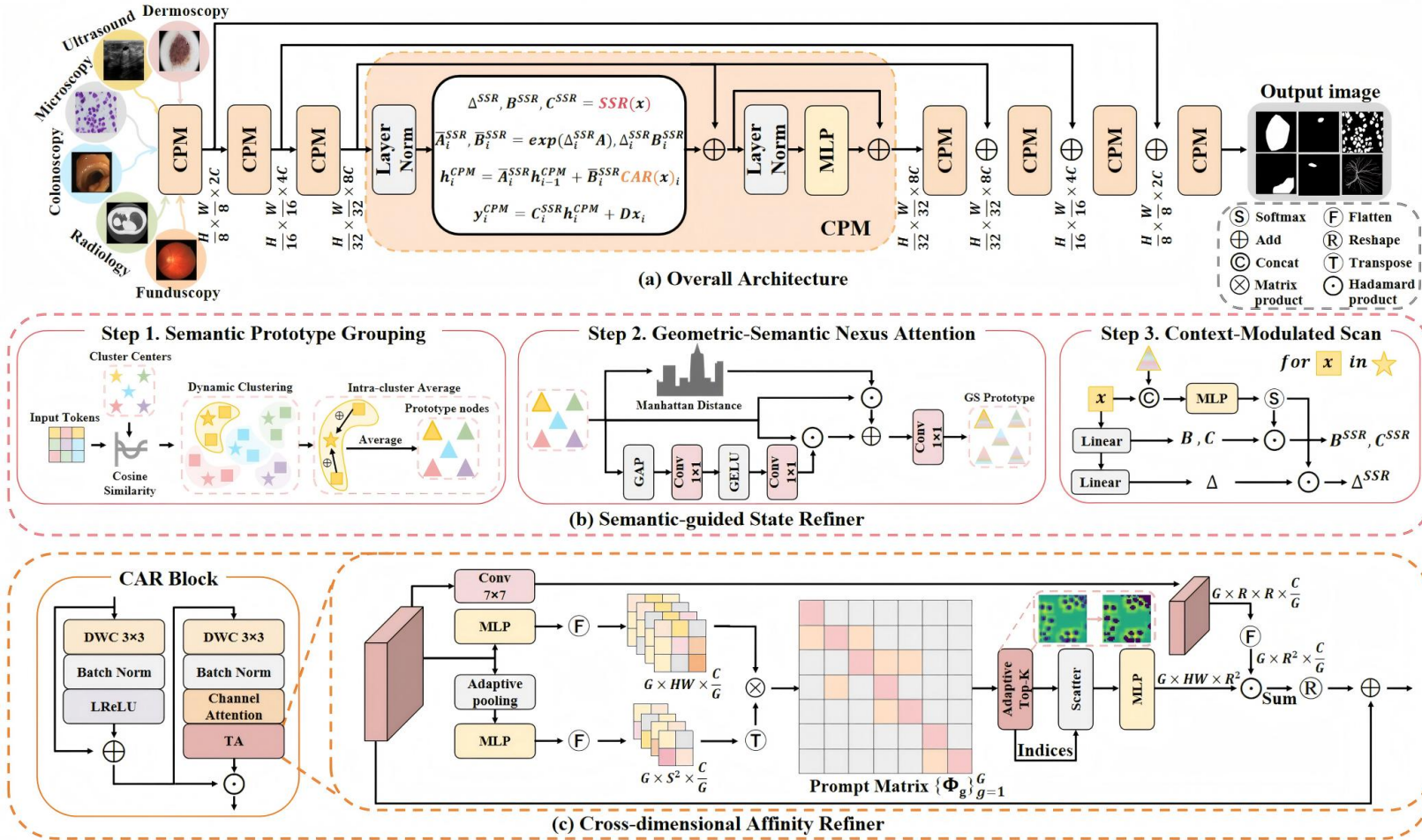


We present **GeoSemba**, a Mamba-based framework for medical image segmentation.

Reconstructs the state-space update rather than only redesigning scan paths.

Couples geometric-semantic propagation with selective spatial-channel interaction within a single scan.

# Overall framework of GeoSemba



$$\Delta^{SSR}, B^{SSR}, C^{SSR} = SSR(x),$$

$$\bar{A}_i^{SSR}, \bar{B}_i^{SSR} = \exp(\Delta_i^{SSR} A), \Delta_i^{SSR} B_i^{SSR}$$

$$h_i^{CPM} = \bar{A}_i^{SSR} h_{i-1}^{CPM} + \bar{B}_i^{SSR} CAR(x)_i,$$

$$y_i^{CPM} = C_i^{SSR} h_i^{CPM} + Dx_i.$$

Overview of GeoSemba, highlighting the core Cross-Paradigm Module (CPM). CPM consists of two key components: the Semantic-guided State Refiner (SSR) and the Cross-dimensional Affinity Refiner (CAR).

# Comparison with State-of-the-art Models

Table 1. Quantitative comparison of GeoSemba with SOTA methods and ablation studies across six diverse medical modalities. The best and second-best results are highlighted in **red** and **blue**, respectively. P-values from one-tailed t-tests are also provided to assess the statistical significance of GeoSemba’s improvements over competitors.

Methods	Dermoscopy		Radiology		Ultrasound		Microscopy		Colonoscopy		Fundus		P-value
	ISIC2018 [9]		COVID19-1[19]		BUSI [1]		DSB2018 [3]		ClinicDB [2]		DRIVE [31]		
	DSC	IoU	DSC	IoU	DSC	IoU	DSC	IoU	DSC	IoU	DSC	IoU	
UNet [27]	87.3	80.2	47.7	38.6	69.5	60.2	91.1	84.3	76.5	69.1	81.4	73.2	2.1E-07
TransUNet [5]	87.3	81.2	75.6	68.8	75.5	68.4	91.8	85.2	87.4	82.9	81.5	74.7	1.8E-06
MADGNet [25]	90.2	<b>83.7</b>	<b>83.7</b>	<b>76.8</b>	81.3	73.4	92.0	85.5	93.9	89.5	85.2	78.3	3.2E-03
PVT-EMCAD [26]	<b>90.9</b>	83.4	83.6	76.5	<b>81.8</b>	<b>73.5</b>	<b>92.7</b>	85.7	<b>95.2</b>	<b>90.4</b>	86.3	80.1	4.7E-03
VM-UNet [28]	89.7	81.4	80.0	74.1	79.2	72.1	91.5	84.6	91.9	86.8	84.0	78.2	1.1E-04
SegMamba [37]	90.4	83.2	82.9	75.6	81.3	72.7	92.0	85.1	91.2	86.1	85.6	79.3	5.6E-03
Spatial-Mamba [36]	90.1	82.5	83.3	76.1	81.2	73.0	91.9	84.9	91.8	86.6	85.8	79.6	2.8E-03
LocalMamba [17]	88.4	82.6	82.7	75.4	80.8	72.6	91.9	85.0	91.1	86.5	85.1	78.5	5.3E-05
Mamba-Sea [7]	89.6	82.9	82.9	75.7	80.7	72.5	92.4	<b>85.9</b>	92.6	87.3	85.7	79.8	2.8E-04
MambaIRv2 [14]	90.5	83.5	83.0	75.8	81.2	73.2	92.0	85.3	92.1	87.0	<b>86.5</b>	80.1	6.1E-03
SCSegamba [22]	90.7	<b>83.7</b>	83.3	75.9	81.5	<b>73.5</b>	92.5	85.8	92.3	87.2	<b>86.6</b>	80.3	1.9E-03
2DMamba [44]	90.2	83.1	82.7	75.6	81.0	73.1	91.3	84.4	91.5	86.7	85.4	79.7	4.4E-03
DefMamba [23]	90.4	83.6	82.8	75.7	81.1	73.3	91.6	84.6	91.7	86.9	85.8	<b>80.6</b>	7.2E-03
GeoSemba(w/o CAR)	90.5	82.7	82.6	75.9	81.5	72.3	91.9	85.5	92.7	88.0	85.0	80.3	2.3E-03
GeoSemba(w/o SSR)	90.7	82.9	82.5	75.7	81.8	72.9	92.4	85.7	93.3	88.6	85.4	80.6	3.6E-03
GeoSemba	<b>91.1</b>	<b>84.1</b>	<b>83.8</b>	<b>77.0</b>	<b>82.1</b>	<b>73.7</b>	<b>93.2</b>	<b>86.6</b>	<b>94.8</b>	<b>90.6</b>	<b>86.6</b>	<b>81.2</b>	-

# Comparison with State-of-the-art Models

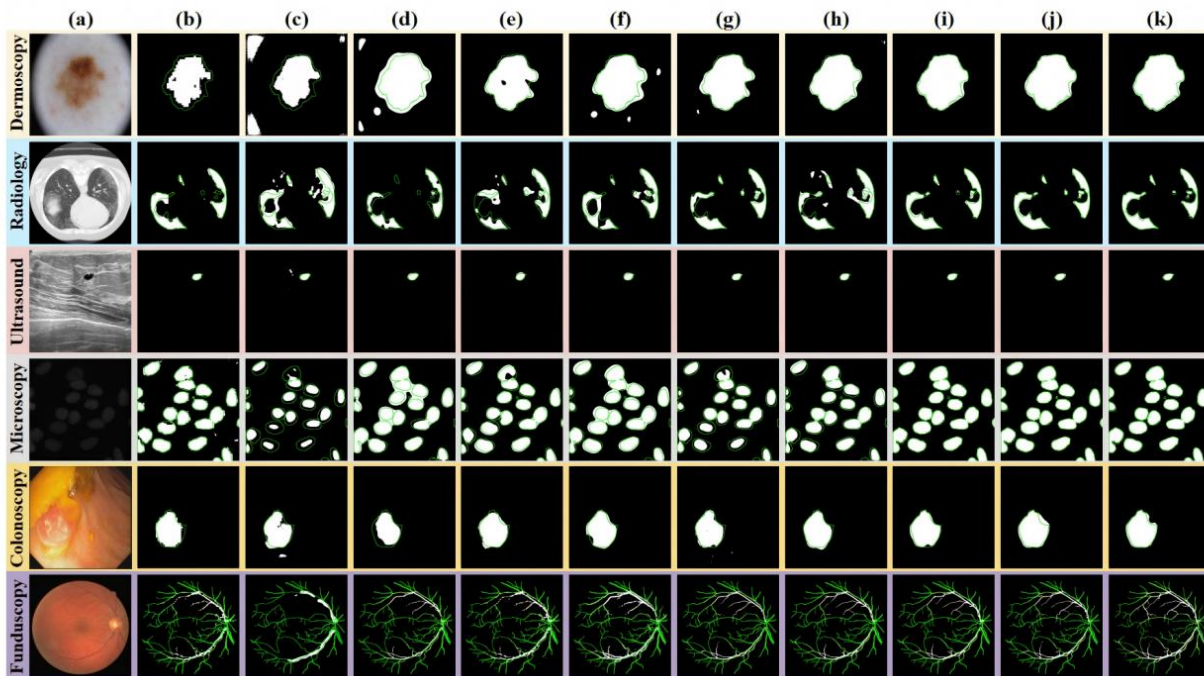


Figure 4. Qualitative comparison of different methods. (a) Input images. (b) UNet [27]. (c) TransUNet [5]. (d) VM-UNet [28]. (e) LocalMamba [17]. (f) MambaIRv2 [14]. (g) SCSegamba [22]. (h) DefMamba [23]. (i) GeoSemba (w/o CAR). (j) GeoSemba (w/o SSR). (k) GeoSemba (ours). Green lines denote the boundaries of the ground truth.

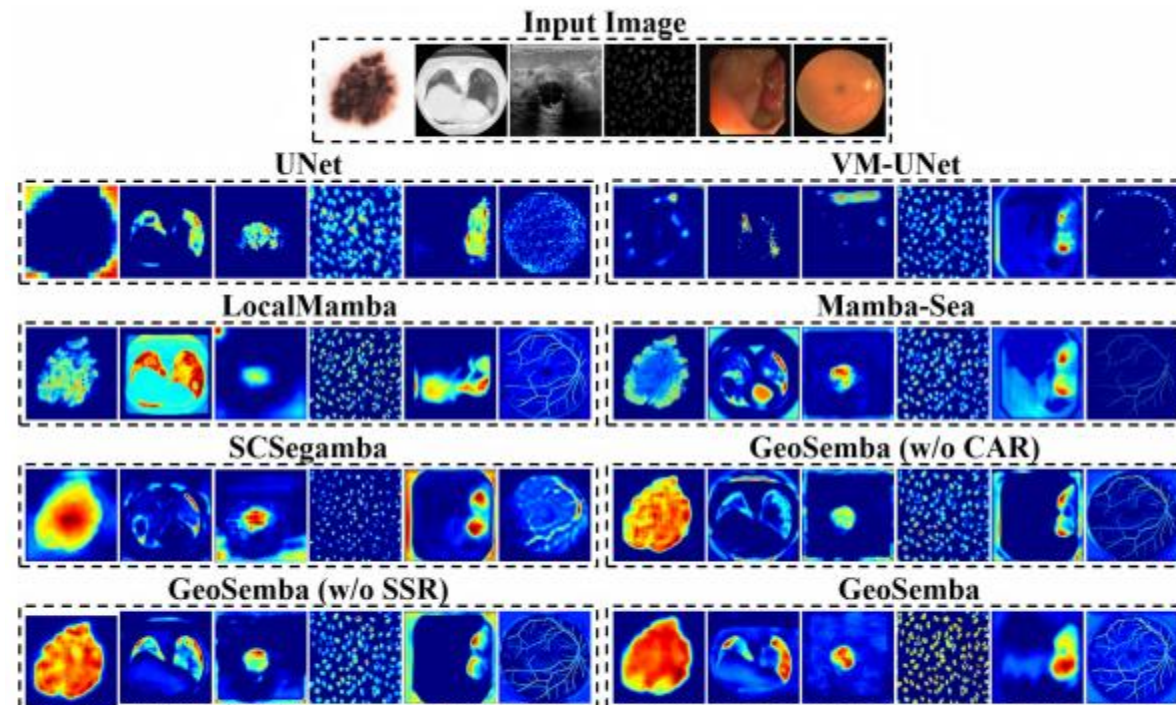


Figure 5. The Grad-CAM visualization of different methods.

Table 2. Ablation study on the components of SSR.

Strategy	ISIC2018	COVID19-1	BUSI	DSB2018	ClinicDB	DRIVE
w/o SPG	88.6	81.1	80.2	90.4	91.5	83.7
w/o GSNA	88.3	80.5	79.9	90.0	91.1	83.2
Full	<b>90.5</b>	<b>82.6</b>	<b>81.5</b>	<b>91.9</b>	<b>92.7</b>	<b>85.0</b>

Table 3. Ablation study on the number of prototype nodes in SSR.

$M$	ISIC2018[9]		COVID-19[19]		BUSI[1]		Params (M)	Infer (ms)
	DSC	IoU	DSC	IoU	DSC	IoU		
3	89.2	82.3	82.1	75.6	80.3	71.8	38.92	14.3
7	<b>91.1</b>	<b>84.1</b>	<b>83.8</b>	<b>77.0</b>	<b>82.1</b>	<b>73.7</b>	41.11	17.0
12	90.1	83.1	83.1	76.3	81.6	73.1	44.67	19.8

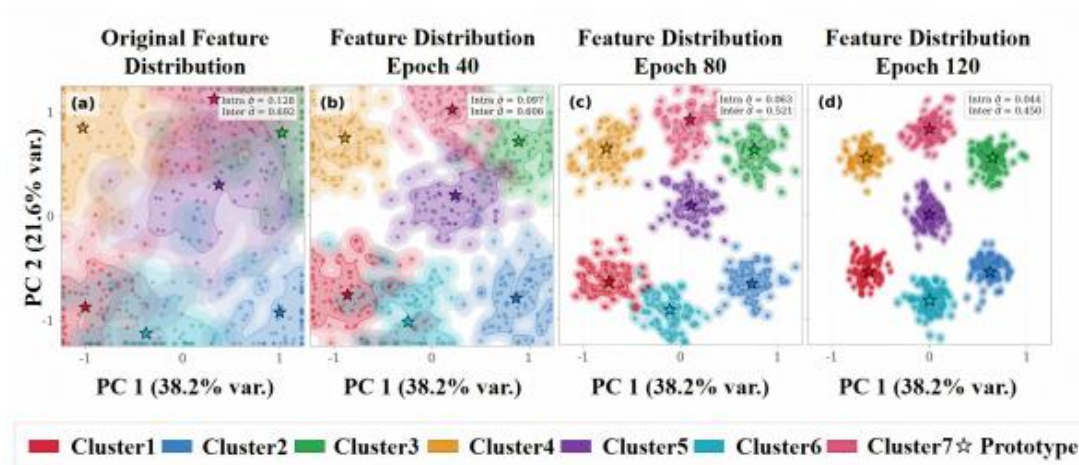


Figure 7. Prototype-guided feature distribution during training.

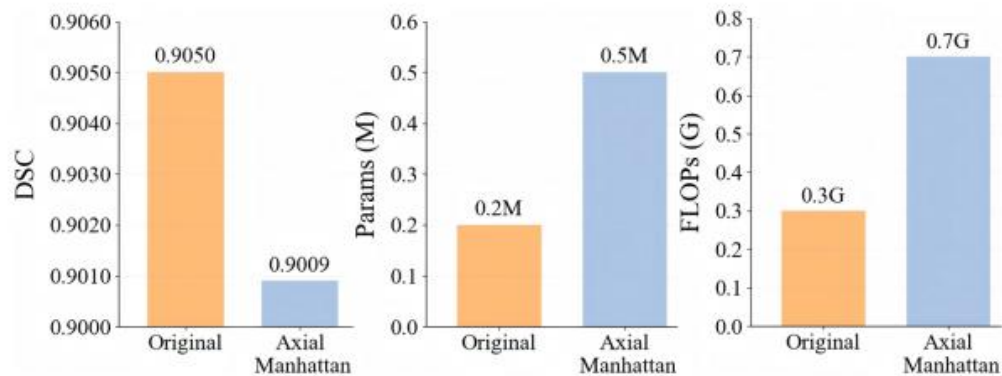


Figure 3. Comparison of GeoSemba with axial decomposition-based methods in terms of DSC, Params, and FLOPs.

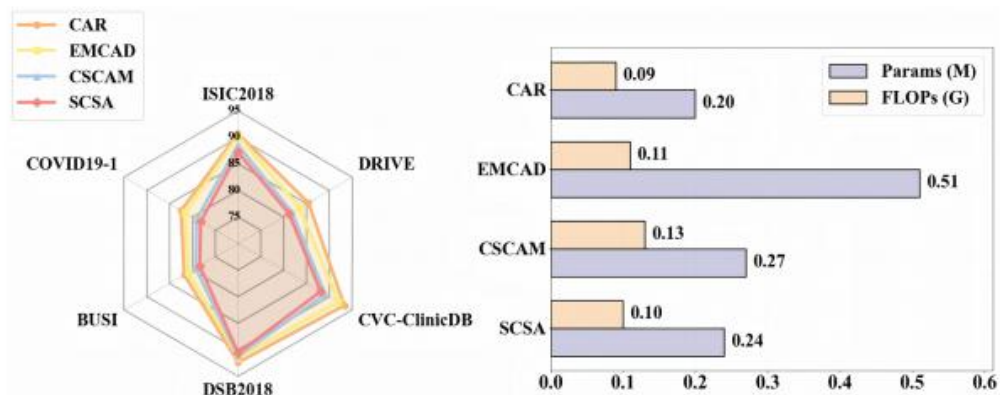


Figure 8. Segmentation performance and computational efficiency of GeoSemba and representative spatial-channel aggregators.

Table 4. Ablation study on the components of CAR.

Strategy	ISIC2018	COVID19-1	BUSI	DSB2018	ClinicDB	DRIVE
w/o MP	88.4	80.6	80.0	90.8	90.8	82.7
w/o CA	88.6	80.9	80.1	91.1	91.0	83.1
w/o Top- $K$	89.8	81.4	80.4	91.9	92.6	84.7
w/o $W^d$	90.3	81.8	80.7	92.1	92.8	85.0
Full	<b>90.7</b>	<b>82.5</b>	<b>81.8</b>	<b>92.4</b>	<b>93.3</b>	<b>85.4</b>

Table 5. Ablation study on the number of channel groups in CAR.

$G$	ISIC2018[9]		COVID-19[19]		BUSI[1]		Params (M)	Infer (ms)
	DSC	IoU	DSC	IoU	DSC	IoU		
6	89.5	82.6	82.7	75.8	81.1	72.4	40.73	15.8
12	<b>91.1</b>	<b>84.1</b>	<b>83.8</b>	<b>77.0</b>	<b>82.1</b>	<b>73.7</b>	41.11	17.0
18	90.2	83.2	83.0	76.3	81.5	73.0	41.58	18.4

Table 6. Ablation study on the Top- $K$  ratio in CAR.

$K$	ISIC2018[9]		COVID-19[19]		BUSI[1]		Params (M)	Infer (ms)
	DSC	IoU	DSC	IoU	DSC	IoU		
0.25	90.0	83.2	83.1	76.3	81.7	73.0	41.05	16.4
0.50	<b>91.1</b>	<b>84.1</b>	<b>83.8</b>	<b>77.0</b>	<b>82.1</b>	<b>73.7</b>	41.11	17.0
0.75	90.3	83.4	83.4	76.6	81.8	73.3	41.30	18.2

# Gradient Flow under Top-K Sparsification

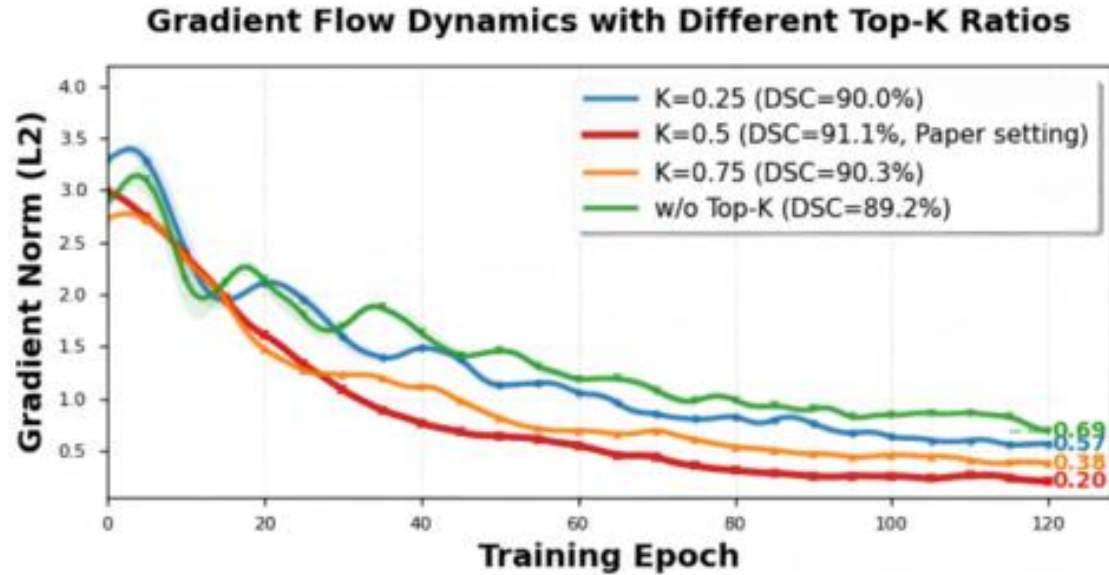


Figure 10. Non-zero gradients under different Top- $K$  settings

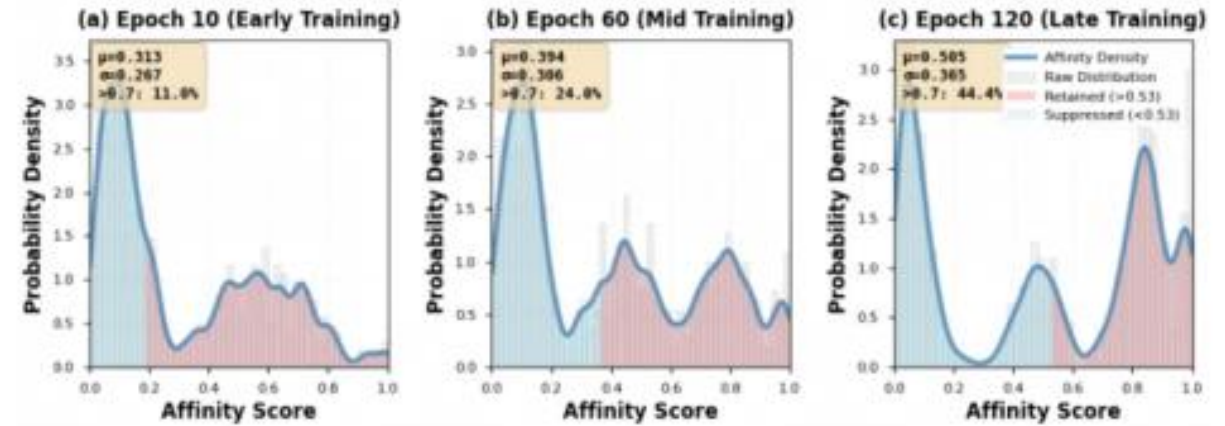


Figure 11. Visualization of affinity patterns at different training stages under Top- $K$  sparsification.

Table 8. Ablation study of BCE/Dice loss weighting ratios on representative medical segmentation benchmarks.

Loss Ratio ( $\alpha:\beta$ )	ISIC2018[9]		COVID19-1[19]		BUSI[1]	
	DSC (%)	IoU (%)	DSC (%)	IoU (%)	DSC (%)	IoU (%)
Dice	88.9	81.6	81.2	74.0	80.7	72.1
BCE	89.3	81.9	81.5	74.2	81.0	72.4
1:1	<b>91.1</b>	<b>84.1</b>	<b>83.8</b>	<b>77.0</b>	<b>82.1</b>	<b>73.7</b>
1:2	90.6	83.2	83.0	76.3	81.8	73.3
2:1	90.4	83.1	82.9	75.8	81.5	73.0

$$\mathcal{L}_{\text{BCE}} = -\frac{1}{N} \sum_{i=1}^N [y_i \log(\hat{y}_i) + (1 - y_i) \log(1 - \hat{y}_i)]$$

$$\mathcal{L}_{\text{Dice}} = 1 - \frac{2 \sum_{i=1}^N y_i \hat{y}_i + \epsilon}{\sum_{i=1}^N y_i^2 + \sum_{i=1}^N \hat{y}_i^2 + \epsilon}$$

$$\mathcal{L}_{\text{total}} = \alpha \mathcal{L}_{\text{Dice}} + \beta \mathcal{L}_{\text{BCE}}$$

# Computational scalability analysis

Table 7. Asymptotic complexity comparison of representative token mixers.

Method	Complexity
Global Self-Attention	$\mathcal{O}(N^2)$
Local / Window Attention (window size $w$ tokens)	$\mathcal{O}(Nw)$
Multi-Directional Mamba ( $k$ scans)	$\mathcal{O}(kN)$
<b>CPM (SSR + CAR)</b>	$\mathcal{O}(N)$

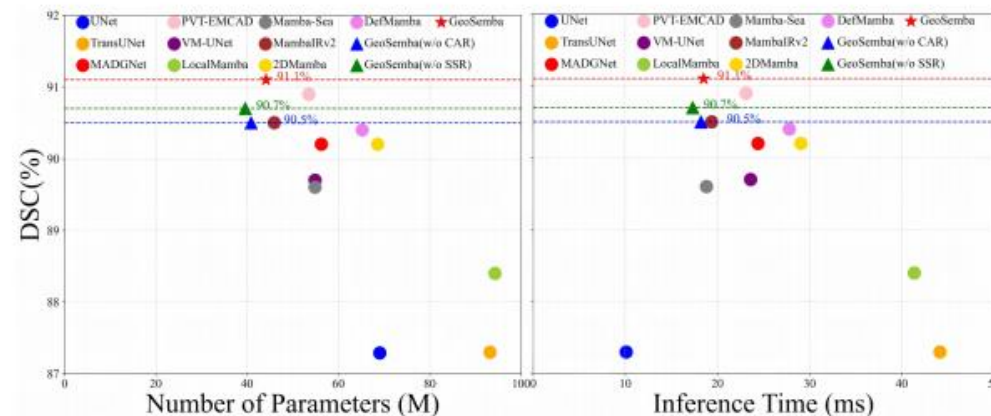


Figure 6. Comparison of parameters and inference speed vs DSC performance for ISIC2018 [9].

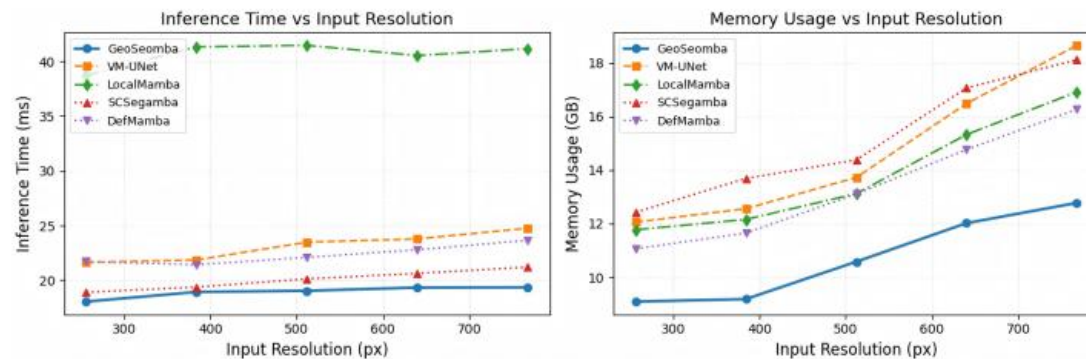


Figure 9. Computational scalability analysis of GeoSemba and representative Mamba variants under different input resolutions.

**Thank you !**