



Generalizable

Radio-Frequency Radiance Fields

for Spatial Spectrum Synthesis

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1 THE PROBLEM

Wireless systems run on data we cannot afford to collect



5G, 6G, WiFi — everywhere

Networks anchor smart cities, healthcare, and sensing pipelines.



Sensing needs dense RF data

DNN-based localization and channel models are data-hungry.



Site surveys are the bottleneck

Measuring spectra at thousands of locations is slow, costly, manual.

1 WHAT WE SYNTHESIZE

Spatial spectrum: power across all directions at a receiver

From the receiver's antenna array, signal arrives from many directions at once.

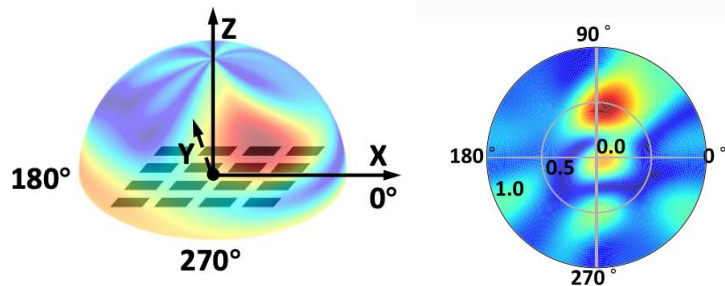
Power per direction (azimuth, elevation) forms a 2D heatmap on the unit sphere.

Why downstream tasks care

Angle of Arrival estimation

Localization, beam steering, channel modeling

A faithful spectrum drives the rest of the wireless stack.



3D sphere view (a) and 2D projection (b) of one spatial spectrum.

Today's RF NeRFs train one model per scene



RAY TRACING

Needs CAD models

Accurate geometry is rarely available and the cost is prohibitive.



NeRF² / NeWRF

Scene-specific MLP

Overfits the training scene; new layout means retraining from scratch.



3DGS-BASED

Faster, still single-scene

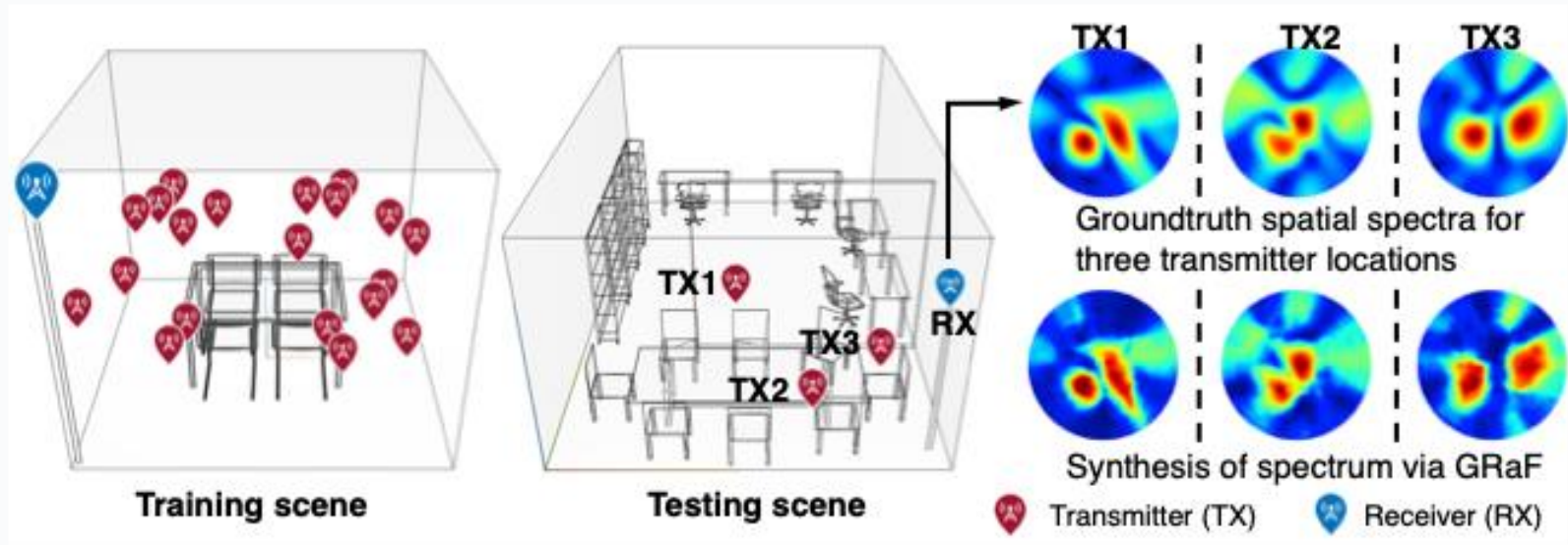
Improves speed within a scene, no cross-scene generalization.



Every new room, every new layout — retrain. The bottleneck just moved.

3 WHAT WE WANT

Synthesize spectra at any transmitter location, in any scene



Train once on a scene — synthesize spectra for new transmitter positions, even when the room itself changes.

Spectra of nearby transmitters interpolate the target

Theorem 1 (Spectrum Interpolation)

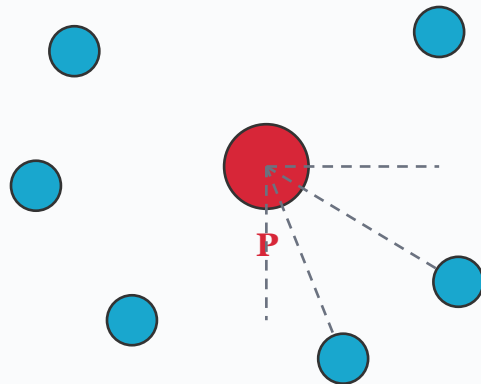
For a target transmitter at \mathbf{P} with L nearest neighbors:

$$\mathbf{SS}(\mathbf{P}) \approx \sum w_i \mathbf{SS}_i$$

Error bound: $\varepsilon \leq K \cdot \delta^2$

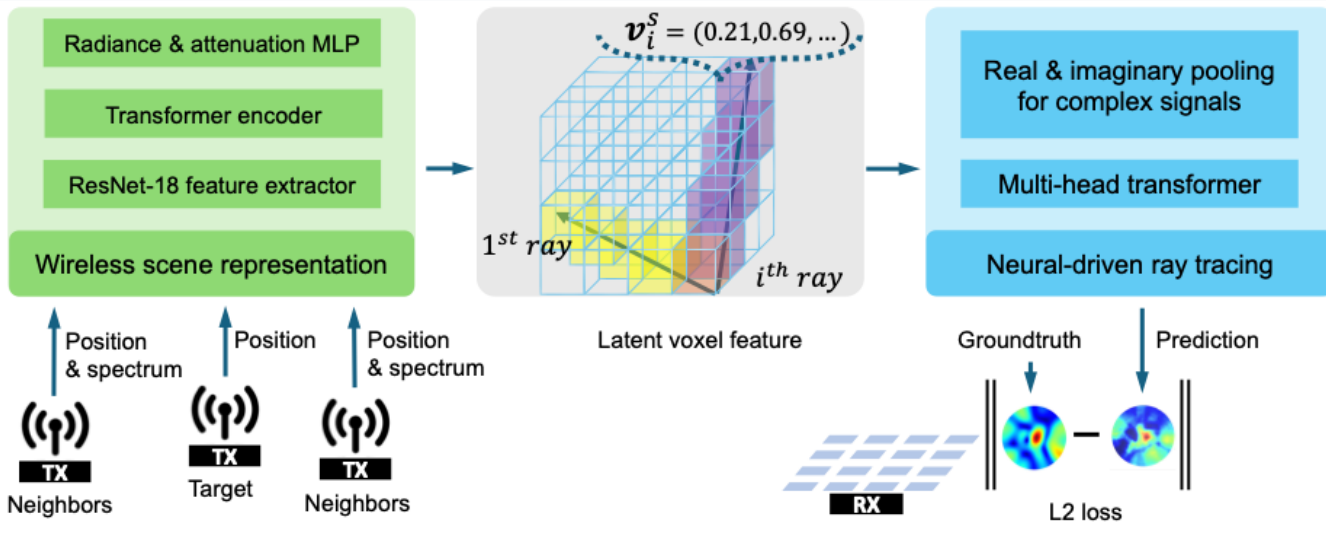
δ = neighborhood radius · K = environment curvature

Smaller neighborhoods \rightarrow tighter approximation.



Target P (red) is interpolated from its L nearest neighbor transmitters (teal).

Two components: a latent RF radiance field + neural ray tracing



① Latent RF radiance field

Geometry-aware Transformer over neighbor spectra

② Neural ray tracing

Complex-valued aggregation per direction

Encode neighbor spectra + geometry into a latent Z



ResNet-18 over each neighbor spectrum

Captures directional power patterns per neighbor.



Positional embedding of $(P_i - P)$

Preserves geometry between target and neighbors.



Geometry-aware Transformer + cross-attention

Dynamically weights neighbors — non-linear interpolation.



Two MLPs \rightarrow latent $Z \in \mathbb{R}^d$

Encodes path loss, multipath, reflection, diffraction.

WHAT Z ENCODES

Path loss

Shadowing

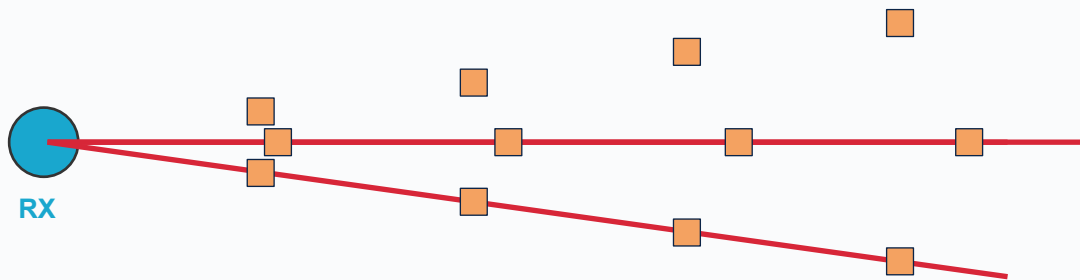
Reflection

Diffraction

Scattering

Multipath

Trace rays from the receiver, aggregate complex contributions



PER VOXEL

Complex radiated signal
+ complex attenuation

$MLP_s(v_s), MLP_a(v_s)$

Per ray r — aggregate complex signal across S samples

$$\mathbf{y}_r = \sum_s (\prod_j \mathbf{a}_j) \cdot \mathbf{s}_s \cdot (\lambda / 4\pi d_s) \cdot \mathbf{e}^{-j2\pi f d_s / c}$$

$$\rightarrow \mathbf{SSO}(\mathbf{r}) = |\mathbf{y}_r|^2$$

complex signal

+ amplitude/phase attenuation

+ free-space path loss and phase shift

PER RAY

Multi-head transformer treats voxels as tokens — attention = cumulative attenuation.

Datasets, baselines, and four image-style metrics

DATASETS

RFID

915 MHz, 4×4 array, 6,123 TX locations (from NeRF²)

MATLAB

Conference + Office layouts × 3 versions each — chairs/tables vary

Extras

Bedroom, outdoor, multi-band (928 MHz, 2.4 GHz, 5.8 GHz)

BASELINES

KNN

Average neighbor spectra

KNN-DL

Per-pixel learnable weights

NeRF²

Scene-specific RF NeRF (= NeWRF without DoA)

METRICS

MSE ↓

Domain loss across directions

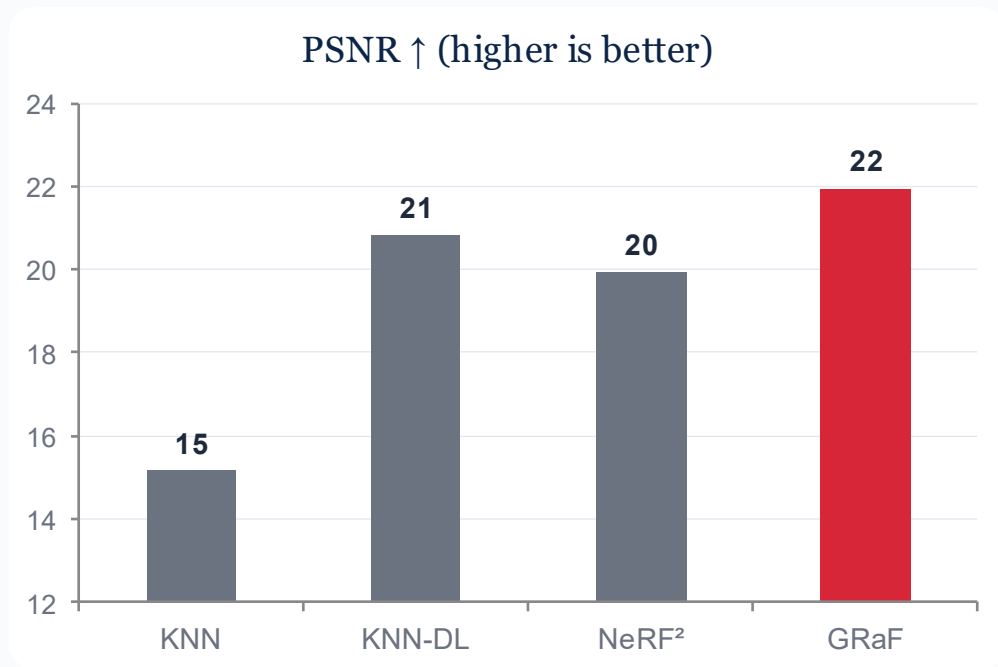
LPIPS ↓

Perceptual similarity

PSNR ↑ · SSIM ↑

Pixel + structural quality

Best across all four metrics in single-scene training



+44.7%

PSNR vs KNN

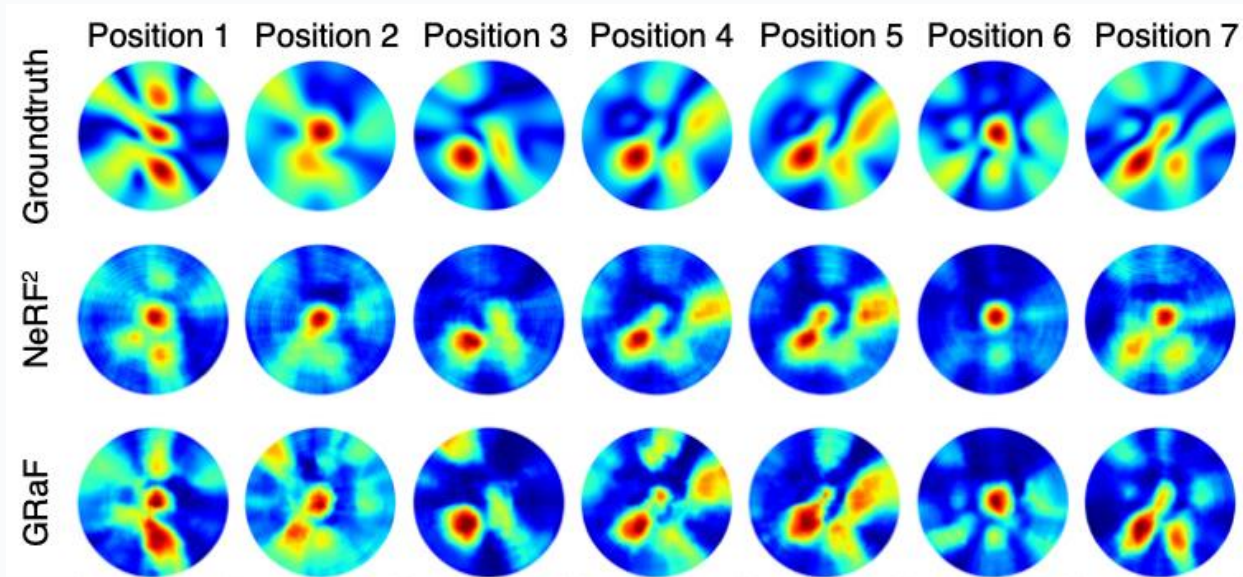
+10.2%

PSNR vs NeRF²

-50.4%

LPIPS vs NeRF²

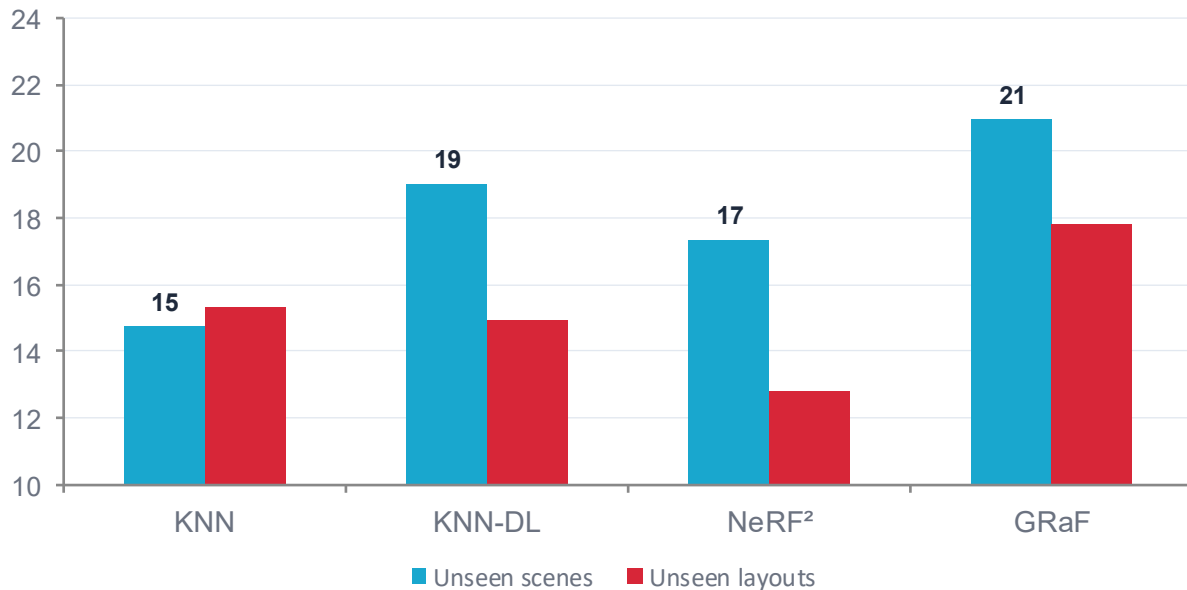
Spectra synthesized by GRaF visibly track ground truth



NeRF² blurs directional peaks. GRaF preserves the heatmap structure at seven held-out transmitter positions.

GRaF holds up where baselines collapse

PSNR \uparrow across two generalization regimes



UNSEEN SCENES

PSNR drops:

-8.5% KNN-DL

-12.9% NeRF²

Best GRaF

UNSEEN LAYOUTS

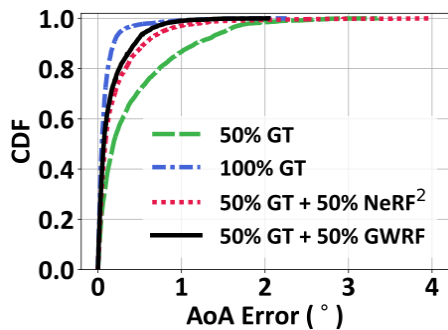
Bigger drops:

-28.2% KNN-DL

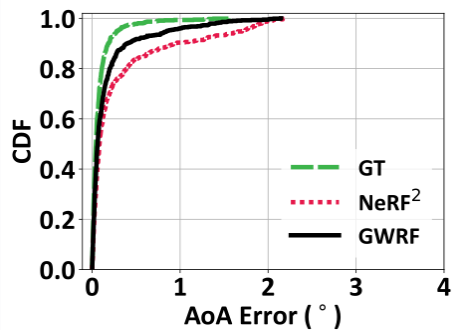
-35.9% NeRF²

Robust GRaF

Synthetic spectra train better AoA estimators



(a) For AANN training



(b) For AANN testing

AoA-error CDF when training (a) and testing (b) an AANN on synthesized spectra.

vs 50% GT only

-61.6%

AoA estimation error when GRaF spectra augment training data.

vs NeRF²-augmented

-25.8%

Lower AoA error than the NeRF²-augmented baseline.

GRaF, in three lines



Theory first

An interpolation theorem in the RF domain — error bounded by neighborhood radius squared.



Architecture follows

Geometry-aware Transformer learns the interpolation; neural ray tracing aggregates complex contributions.



Generalization works

State-of-the-art across single-scene, unseen scenes, unseen layouts, and a downstream AoA task.